Design Optimization Using Soft Computing Techniques For Extrusion Blow Molding Processes

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Abstract
The control of thickness distribution in extrusion blow molded parts is critical to assure product quality and reduce manufacturing cost. This study applies the soft computing strategy to determine the optimal die gap in the parison programming of extrusion blow molding process. Two types of optimization problem are addressed in this study. The process optimization objective is obtaining a uniform thickness of blown parts, and the design optimization objective is minimizing part weight subject to stress constraints. The finite element software, BlowView, is used to simulate the parison extrusion and the blow molding processes. However, the simulations are time consuming, and minimizing the number of simulation becomes an important issue. The proposed strategy, Fuzzy Neural-Taguchi and Genetic Algorithm (FUNTGA), first establishes a back propagation network using Taguchi’s experimental array to predict the relationship between the design variables and the response. Genetic algorithm is then applied to search for the optimum design of parison programming. As the number of training samples is greatly reduced due to the use of orthogonal arrays, the prediction accuracy of the neural network model is closely related to the distance between sampling points and the evolved designs. The Reliability Distance is proposed and introduced to the Genetic Algorithm using fuzzy rules to modify the fitness function and thus improve search efficiency. The design of a HDPE bottle is used to illustrate the application of the process optimization, and the design of a gas tank is used to illustrate the application of performance. The design optimization uses ANSYS to find the stress distribution of blown parts under loads. The comparison of results using the optimization module of BlowView, Taguchi, and FUNTGA demonstrates the effectiveness of the proposed strategy.

Keywords: Fuzzy logics, Neural Network, Genetic Algorithm, Taguchi, Multidisciplinary Design Optimization

1 Introduction
Extrusion blow molding is a low cost manufacturing process for complex hollow parts [1]. The process involves complex procedures such as parison extrusion, clamping, blow up, and cooling. First, the parison extrusion produces a molten thermoplastic tube coming out from the die. Once extrusion is finished, the parison is clamped and high-pressure air is blown into it to get the final part. To control the parison thickness over time, there is a mandrel that can move in and out to the die (Fig.1). Obviously, the parison thickness determines the thickness of the inflated part. The function of the parison programming is manipulating the die gap openings to obtain the desired thickness distribution of blown parts.

The programming points are specified by the extrusion time and the die gap opening of the parison. As the example part shown in Fig.2, we identify the die gap openings at 7 discrete extrusion times as the design variables: \( P(t_0), P(t_1), P(t_2), P(t_3), P(t_4), P(t_5), \) and \( P(t_6) \). These design variables will be adjusted to obtain the desired thickness distribution of blown parts. Two types of optimization problem are often encountered in the design of blow-molded parts by controlling the die gap programming. The process optimization objective is targeting a uniform part...
thickness distribution of blown parts, and the design optimization objective is minimizing part weight subject to stress constraints.

![Figure 1: The control of the parison thickness using the parison programming](image1)

![Figure 2: Programming points of parison extrusion](image2)

Lee et al. [4] used a finite element model of thin film to simulate blow molding processes, and applied the feasible direction method to minimize the parison volume at the constraints of part thickness. Diraddo et al. [2] established a neural network to predict the distribution of parison thickness and applied Newton-Raphson method to obtain the final blow molded part specifications [3]. However, the investigation of the relationship between design variables and the wall thickness distribution of blown parts requires expensive experiments and time-consuming simulations. To reduce the number of experiments and simulations, an efficient strategy of data analysis is essential.

In this study, we apply an optimization strategy based on Taguchi’s experimental design [5] and soft computing techniques [6] to the optimization of parison programming to obtain the required thickness distribution. The proposed strategy establishes a local neural network based on Taguchi’s orthogonal array experiments and assumes the fuzzy inference to genetic algorithm to search for the optimal operating conditions. The finite element software, BlowSim [8], is used to simulate the parison extrusion and the blow molding processes.

The design of a gas tank targeting a uniform part thickness distribution illustrates the application of the proposed method to the process optimization. For the blown parts subjected to external and internal loading, an adequate part thickness profile has to be determined to satisfy the part mechanical performance. The aim is then to find the optimal die gap programming that will minimize the part weight and satisfy the part mechanical performance as well.

## 2 Optimization Strategy

Taguchi’s method has proven its efficiency and simplicity in parameter design. The proposed optimization strategy, FUzy Neural-Taguchi with Genetic Algorithm (FUNTGA) [10], applies Taguchi’s experimental design to the training and testing of a neural network model. The trained network becomes the function generator of the design fitness in the Genetic Algorithm. The optimum search using GA enhances the possibility for a better design than the conventional analysis of means (ANOM). A fuzzy inference of engineering knowledge is introduced to enhance the searching efficiency of GA. The flowchart of the optimization strategy is illustrated in Fig.3.

### 2.1 Taguchi’s Method

Inspired from statistical factorial experiments, Taguchi’s method features orthogonal arrays and analysis of mean (ANOM) to analyze the effects of design variables. Each variable is assumed to have finite levels (set points), such as two or three levels, within the investigating range. The orthogonal array is a type of fractional factorial experiments. The application of orthogonal arrays reduces the number of experiments, which is particular effective for design optimization involving expensive experiments or time-consuming simulations. For instance, instead of 27 experiments for three 3-level full factorial experiments, the L9 orthogonal array selects only nine treatments. ANOM study of experiment results reveals the effects of design parameters that are used to determine the optimal
level of each parameter. Knowing that Taguchi’s result is not a global optimum, however iterations of Taguchi’s method can provide a solution near to the optimum design.

Taguchi’s approach utilizes ANOM of fractional factorial experiments to predict the optimal design of the full factorial experiments. However, the prediction of the optimal design is sensitive to the selection of factorial levels and interaction effects. Also, the restriction of parameter values to factorial levels reduces the possibility of having better designs between preset levels.

**Figure 3 The Optimization flowchart of FUNTGA**

**Figure 4 Full factorial and fractional factorial experiments for three variables**

### 2.2 Neural-Taguchi network

Neural network technologies are effective in process control. The network is used to set up a simulation model for a complex nonlinear system. The back propagation network (BPN) is a type of supervised learning networks. Sampling data are divided into learning and testing samples. Learning samples are used to determine the weighting matrices, $W_{ij}$ and $W_{j\alpha}$, among neurons and testing samples to determine the accuracy and the generality of the network.
Training samples are essential to the prediction quality of network models. This study employs Taguchi’s experimental design to select training samples to reduce the number of experiments and to maintain a good sample representation [7][9]. The steepest gradient method is assumed to train the weighting matrices. The verification experiment of the optimal design from the ANOM study will serve as a testing sample. The trained network can accurately predict responses for the parameter designs between factorial levels. Significant interactions often introduce complexity to experimental design and lead to erroneous prediction of optimal factorial levels. The network model can resolve interaction effects among variables. These features enable the network to explore a better design as compared with Taguchi’s additive model [5].

2.3 The search for the optimum of the Neural-Taguchi network

The trained Neural-Taguchi network can predict responses for the parameter combinations in the investigating range. Generic Algorithm is thus applied to search for the optimum. If the verification result of the predicted optimum is not satisfactory, the design will be used as an initial design and another set of orthogonal array experiments will be conducted. The results will be served as additional testing data for the network. The iteration process stops when the predicted optimum obtained from GA and the network converges.

The Neural-Taguchi network replaces Taguchi’s additive model to predict design outputs. The search for the optimum in the investigating range using GA will explore the possibility of better designs other than factorial points. However, the application of orthogonal arrays significantly reduces the number of training samples as compared with conventional random sampling. Owing to that better prediction accuracy will exist around sampling points, our approach introduces a fuzzy inference to steer the search direction of GA.

2.3.1 Normalization of design parameters

To facilitate the calculation of the distance among designs, the values of the set points of continuous variable $x_k$ are normalized to $z_{ik}$ using the following transformation

$$z_{ik} = \frac{(x_{ik} - \frac{\text{max}(x_k) + \text{min}(x_k)}{2})}{\frac{\text{max}(x_k) - \text{min}(x_k)}{2}}$$  \hspace{1cm} (1)

where $\text{max}(x_k)$ represents the maximum and $\text{min}(x_k)$ represents the minimum values of the factorial variable $x_k$. Thus the normalized factorial values of an equal spaced three-level continuous variable, $x_1$, will become $(z_{11}, z_{12}, z_{13}) = (-1, 0, 1)$. For discrete variables, the factorial values are equally assigned between -1 and +1.

2.3.2 The Reliability Distance

The mean Euclid distances between predictive designs, $D_i$, and the sample data $S_j$ are defined as follows

$$r_j = \left[ \frac{1}{n} \sum_{k=1}^{n} (D_{ik} - S_{jk})^2 \right]^{0.5}$$  \hspace{1cm} (2)

where $n$ represents the number of variables.

Since predictions around the sampling points of the trained network will have higher accuracy, we proposed to use the Reliability Distance of a predictive design as the minimum factorial distance between the prediction and sampling data.

$$RD_i = \min(r_j)$$  \hspace{1cm} (3)

Smaller $RD$ results in higher prediction accuracy. Also, the distance of an interpolating design is assumed negative and the distance of an extrapolating design is assumed positive. For instance, the Reliability Distance of $D_1$ in Fig.5 is negative and the Reliability Distance of $D_2$ is positive.
2.3.3 The fuzzy rules of prediction accuracy

The Reliability Distance of a predictive design determines the Prediction Reliability (PR) of the design. The reliability of the predicted design decreases when the absolute value of RD increases. Also, the reliability of extrapolating designs is often much worse than the interpolating designs. Based on the above characteristics of neural network, we propose to use fuzzy rules of the design reliability as follows:

- **R1**: If $RD$ is PB then prediction reliability is Bad
- **R2**: If $RD$ is PM then prediction reliability is Poor
- **R3**: If $RD$ is PS then prediction reliability is Fair
- **R4**: If $RD$ is ZE then prediction reliability is Excellent
- **R5**: If $RD$ is NS then prediction reliability is Good
- **R6**: If $RD$ is NM then prediction reliability is Fair
- **R7**: If $RD$ is NB then prediction reliability is Poor

Seven levels are defined to describe the condition variables: PB(Positive Big), PM(Positive Medium), PS(Positive Small), ZE(Zero), NS(Negative Small), Negative Medium (NM), and NB(Negative Big). Five levels are defined to describe the assessment results: Excellent, Good, Fair, Poor, and Bad. Standard membership functions associated with these statements are illustrated in Fig.6 and Fig.7. Fig.8 is the reliability contour plot for the two-dimensional case using the fuzzy inference. The solid dots represent the training samples.

2.3.4 Genetic Algorithm

FUNTGA uses the Genetic Algorithm to search the optimum of the Neural-Taguchi network. However, the accuracy of the network is limited due to the reduced number of training samples. The design fitness obtained from the network is thus modified to reflect the characteristics of prediction accuracy. The search of the local optimum will then be restricted to the surroundings of the training samples to prevent the possible erroneous prediction.

$$Fitness_{act} = \begin{cases} Fitness_{net} \times PR, & \text{if } Fitness_{net} > 0 \\ Fitness_{net} / PR, & \text{if } Fitness_{net} < 0 \end{cases}$$  \hfill (4)
3 Optimization of Blow Molding Parameters for Process Design

This work uses the proposed optimization strategy to get the optimal parameter design of extrusion blow molding process for the gas tank case of the Kautex Textron Company. The gas tank is made of High Density Polyethylene (HDPE). The design objective is to target a uniform part thickness of 5 mm. The blow molded part thickness distribution is estimated by using the BlowSim software. Fig. 9 shows that the die gap openings at 13 discrete extrusion times are selected as the control variables: \( P(t_1), P(t_2), ..., P(t_{13}) \).

![Figure 9 The control points of the gas tank example](image)

3.1 The Objective Function

A quality blow molding part requires on-target and uniformly distributed part thickness. To reach this goal, we propose to define an objective function as the average quality loss due to the deviation of thickness,

\[
\text{Avg. Loss} = \frac{\sum_{i=1}^{n} (t_i - T)^2}{n}
\]  

(5)

where \( t_i \) stands for the thickness of node \( i \), \( T \) for the target thickness, and \( n \) for the total number of nodes of the simulation model.

Any deviation from the target thickness will cause quality loss. The average quality loss can be divided into two parts: the mean deviation from the target thickness and the thickness variation around mean as the following
Design Optimization Using Soft Computing Techniques For Extrusion Blow Molding Processes

\[
\frac{\sum_{i=1}^{n}(t_i - \bar{T})^2}{n} = (\bar{T} - T)^2 + \frac{\sum_{i=1}^{n}(t_i - \bar{T})^2}{n} = (\bar{T} - T)^2 + s^2
\]

where \( \bar{T} \) is the mean stress and \( s^2 \) is the sampling variance. Reducing the quality loss leads to a thickness distribution of a smaller variance and a mean thickness closer to the target.

### 3.2 Taguchi’s parameter design

#### 3.2.1 Experimental Design

The die gap openings at 13 discrete extrusion times are selected as the control factors. The design optimization manipulates the die gap openings of programming points to obtain a uniform thickness distribution. The initial design adopts a uniform die gap opening of 10% for first four control points and 20% for the rest. The L36 orthogonal array is selected as the experimental design (Table 1). For each opening, we assume a three-levels variation around the initial design located in the middle of the design space. The range between upper and lower levels represents the design space.

<table>
<thead>
<tr>
<th>Table 1. L36 orthogonal array</th>
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<tr>
<td>1</td>
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<td>8</td>
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<tr>
<td>9</td>
</tr>
</tbody>
</table>

#### 3.2.2 Parameter design

Taguchi’s method applies the analysis of means (ANOM) to estimate parameter sensitivities. Fig.10 represents the factor effects for each die opening on objective. The additive model estimates the optimum treatment combination to be \( A_1B_3C_3D_2E_2F_1G_1H_1I_1J_1K_1L_1M_3 \). The BlowSim simulation of Taguchi’s optimum shows the loss of 6.44, which is not the best design in Table 1. The failure of Taguchi’s approach might due to interactions among design variables and strong system non-linearity.

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3.3 Design optimization using FUNTGA

3.3.1 The establishment of the neural network

FUNTGA provides a more efficient and accurate optimum search using the same experimental data of Taguchi’s experiments. The L36 orthogonal experiments are divided into two smaller orthogonal arrays as differentiated by the shade in Table 1. 18 experiments are used as training samples and the other 18 experiments are used as testing samples. There are 15 neurons in the hidden layer. The initial learning rate is set to 1.0 and the initial momentum term is set to 0.5.

3.3.2 Optimum search using GA

The fuzzy rules for prediction accuracy are applied to GA to improve the searching efficiency. The fitness function is defined as follows,

\[
Fitness_{GA} = \frac{-Avg\_loss}{PR}
\]  

(7)

The trained network will then be used as the function generator for each chromosome combination. The parameters of Genetic Algorithm used in this study are listed in Table 2.

<table>
<thead>
<tr>
<th>Population size</th>
<th>Pool selection style</th>
<th>Scale style</th>
<th>Cross Over rate</th>
<th>Mutation rate</th>
<th>Max iteration</th>
</tr>
</thead>
<tbody>
<tr>
<td>37</td>
<td>Parent and offspring</td>
<td>Linear scale</td>
<td>0.75</td>
<td>0.1</td>
<td>100</td>
</tr>
</tbody>
</table>

The search result of GA will then be added to the training samples of the neural model to further improve the network accuracy. The optimization process iterates until the results converge. The iteration history of FUNTGA is shown in Fig.11.
3.4 Comparison of results

Fig.12 and Table 3 present the die gap openings of the parison programming and the optimization results obtained from Taguchi’s method, BlowOp, and FUNTGA. BlowOp is a BlowSim optimization module that uses a gradient-based algorithm to control the die gap openings of the parison programming points. Although BlowOp optimum provides a mean thickness closer to the target of 5 mm, FUNTGA’s optimum exhibits a more uniform distribution and the lowest quality loss.

<table>
<thead>
<tr>
<th>Iteration</th>
<th>Initial Design</th>
<th>Taguchi’s</th>
<th>BlowOp</th>
<th>FUNTGA’s</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mean</td>
<td>7.40</td>
<td>6.17</td>
<td>5.12</td>
<td>5.63</td>
</tr>
<tr>
<td>Standard Deviation</td>
<td>2.39</td>
<td>2.25</td>
<td>2.07</td>
<td>1.74</td>
</tr>
<tr>
<td>Average Loss</td>
<td>11.48</td>
<td>6.44</td>
<td>4.32</td>
<td>3.42</td>
</tr>
</tbody>
</table>

Figure 12 The optimal designs from various methods

4 Optimization of Blow Molding Parameters for Performance Design

This work applies the proposed optimization strategy to get the optimal parameter design of extrusion blow molding process for the HDPE bottle of the Lear Corporation. Two types of loading will be investigated: an internal pressurization at 110 (psi) and a top displacement of 5 (mm) during 5 seconds as illustrated in Fig.13. The maximum allowable stress, corresponding to the ultimate tensile strength of the material, is set to 33 MPa. For this material, the Young’s modulus is 879 MPa and we assume that the thickness part shrinkage is 3%. From a part thickness distribution obtained from BlowSim, ANSYS software is used to make the structural analysis for the specified loading [11].

4.1 The Objective Function

The initial formulation for this optimization can be represented as follows,

Minimize: Part_Weight(P(tj))
Design Variable: P(tj)
Constraints: s[P(tj), P, T] ≦ σa
Where \( P(t_j) \) are the gap openings of the controlling points, \( s_i \) are the stresses of node \( i \), \( \sigma_a \) is the allowable stress of the material, \( P \) is the internal pressure, and \( T \) is the top displacement.

The objective function is modified to obtain a wall thickness distribution of minimal weight subject to stress constraints. The reduction of an element thickness results in the increase of its stress level. Consequently, the design objective can be replaced by a minimization of the stress variance around the stress mean close to the stress constraint. The smaller variance of the stress distribution, the closer the mean can be moved to the allowable material strength, that leads to thinner elements, and thus minimal part weight. However, any element stress exceeding the allowable strength might result in part failure. In this work the constrained optimization is replaced by an unconstrained minimization of the variance of stress distribution around the allowable stress level using the external penalty method as illustrated in Fig.14.

The objective function (Eq. [8]) contains two portions: the quality loss due to variation of stress distribution and the penalty loss due to constraint violation

\[
MOBJ = \frac{\sum_{i=1}^{n} (s_i - \sigma_a)^2}{n} + \sum_{i=1}^{n} <s_i - \sigma_a>^2
\]

where \( n \) is the total number of nodes of the simulation model.

The quality loss due to variation of stress distribution is estimated by the mean squared deviation of the element stress from the allowable stress level that is similar to the objective used in the previous process optimization. The average quality loss can be divided into two parts: the deviation of the mean stress from the allowable strength and the variation of the stress around mean.

The second portion of the modified objective function, the penalty loss, is estimated using a second order singularity function. This portion accounts for the penalty of elements violating the stress constraint.

\[
<s_i - \sigma_a>^2 = \begin{cases} 
0, \text{ if } s_i \leq \sigma_a \\
(s_i - \sigma_a)^2, \text{ if } s_i > \sigma_a 
\end{cases}
\]

The search for the design of minimum objective function will provide a thickness of minimum part weight while satisfying the stress requirement.

4.2 Taguchi’s parameter design

4.2.1 Experimental Design

The die gap openings at 7 discrete extrusion times are selected as the control factors: \( P(t_0) \), \( P(t_1) \), \( P(t_2) \), \( P(t_3) \), \( P(t_4) \), \( P(t_5) \), and \( P(t_6) \). The initial design adopts a uniform die gap opening of 75%. The L18 orthogonal array is selected as the experimental design. For each opening, we assume a three-levels variation around the initial design located in the middle of the design space. The range between upper and lower levels represents the design space. We assume 40% variation range.

\[
S/N \_ratio = -10 \times \log(MOBJ)
\]

4.2.2 Parameter design

Taguchi’s method applies the analysis of means (ANOM) to estimate parameter sensitivities. Fig.15 represents the factor effects for each die opening on the S/N ratio. A design with higher S/N ratio has a smaller value of the objective function. Taguchi’s additive model estimates the optimum treatment combination to be \( A_1B_1C_1D_1E_1F_1G_1 \). The BlowSim simulation result of Taguchi’s optimum shows a S/N ratio of –27.45 that is worse than the S/N of the initial design of –25.6. The failure of Taguchi’s approach might due to interactions among design variables and strong system non-linearity.
4.3 Design optimization using FUNTGA

4.3.1 Establishment of neural network

FUNTGA uses L18 orthogonal experiments as learning samples for the Back Propagation Network (BPN) of the extrusion blow molding process. The initial design and Taguchi’s optimum design are used as testing samples for the trained network. There are 14 neurons in the first hidden layer and 6 neurons in the second hidden layer. The initial learning rate is set to 1.4 and the initial momentum term is set to 0.5. The RMS error reduces to 0.055 after 16000 epochs.

4.3.2 Optimum search using GA

The fuzzy rules for prediction accuracy are applied to GA to improve the searching efficiency. The fitness function is defined as follows,

\[
Fitness_{GA} = \frac{S}{N \_ratio}/PR
\]

The trained network will then be used as the function generator for each chromosome combination. The parameters of Genetic Algorithm used in this study are listed in Table 4.

<table>
<thead>
<tr>
<th>Table 4 Genetic Algorithm parameters</th>
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<tr>
<td>Population size</td>
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<td>20</td>
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</table>

4.4 Comparison of the results

Fig.16 shows the profiles of optimal die gap openings of parison programming and Table 5 compares the stress distributions of the initial design and the optimal one obtained from Taguchi’s method and FUNTGA strategy. Taguchi’s ANOM approach is disturbed by parameter interactions and system non-linearity. Taguchi’s optimum provides a mean stress closer to the allowable strength 33 MPa. However, the large variance of the stress distribution results in stronger violation of stress constraints than the initial design. FUNTGA’s optimum exhibits a mean thickness close to the allowable and the smallest deviation in three designs, which leads to a design of smaller weight while satisfying the stress constraints. Fig.17 presents the stress distributions of three designs.

5 Conclusions

This study presents how to apply soft computing technology to determine the optimum die gap openings of parison programming of extrusion blow molding process. Taguchi’s method is cost effective to obtain an improved design in a few experiments. However, possible interactions among parameters and system non-linearity could complicate parameter design. Instead of using ANOM of Taguchi’s experimental design, FUNTGA establishes a back propagation network using Taguchi’s experimental data. Heuristic knowledge of prediction accuracy is
applied to GA using fuzzy rules to steer the search direction. The proposed strategy works well with both the process optimization and the performance optimization examples. Extra iterations using FUNTGA’s approach are possible if further improvement is desired. The comparison of results demonstrates the effectiveness of the proposed strategy.

![Figure 16 The optimal designs from various methods](image)

![Figure 17 The comparison of the stress distribution](image)

<table>
<thead>
<tr>
<th>Table 5 The comparison of various optima</th>
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<tr>
<td>Initial</td>
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<td>Taguchi’s</td>
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<td>FUNTGA’s</td>
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