

Chapter 9

9.1a. $1/6$

b. $1/6$

9.2 a $P(\bar{X} = 1) = P(1,1) = 1/36$

b $P(\bar{X} = 6) = P(6,6) = 1/36$

9.3a $P(\bar{X} = 1) = (1/6)^5 = .0001286$

b $P(\bar{X} = 6) = (1/6)^5 = .0001286$

9.4 The variance of \bar{X} is smaller than the variance of X .

9.5 The sampling distribution of the mean is normal with a mean of 40 and a standard deviation of $12/\sqrt{100} = 1.2$.

9.6 No, because the sample mean is approximately normally distributed.

9.7 a $P(\bar{X} > 1050) = P\left(\frac{\bar{X} - \mu}{\sigma/\sqrt{n}} > \frac{1050 - 1000}{200/\sqrt{16}}\right) = P(Z > 1.00) = .5 - P(0 < Z < 1.00) = .5 - .3413 = .1587$

b $P(\bar{X} < 960) = P\left(\frac{\bar{X} - \mu}{\sigma/\sqrt{n}} < \frac{960 - 1000}{200/\sqrt{16}}\right) = P(Z < -.80) = .5 - P(0 < Z < .80) = .5 - .2881 = .2119$

c $P(\bar{X} > 1100) = P\left(\frac{\bar{X} - \mu}{\sigma/\sqrt{n}} > \frac{1100 - 1000}{200/\sqrt{16}}\right) = P(Z > 2.00) = .5 - P(0 < Z < 2.00) = .5 - .4772 = .0228$

9.8 a $P(\bar{X} > 1050) = P\left(\frac{\bar{X} - \mu}{\sigma/\sqrt{n}} > \frac{1050 - 1000}{200/\sqrt{25}}\right) = P(Z > 1.25) = .5 - P(0 < Z < 1.25) = .5 - .3944 = .1056$

b $P(\bar{X} < 960) = P\left(\frac{\bar{X} - \mu}{\sigma/\sqrt{n}} < \frac{960 - 1000}{200/\sqrt{25}}\right) = P(Z < -1.00) = .5 - P(0 < Z < 1.00) = .5 - .3413 = .1587$

c $P(\bar{X} > 1100) = P\left(\frac{\bar{X} - \mu}{\sigma/\sqrt{n}} > \frac{1100 - 1000}{200/\sqrt{25}}\right) = P(Z > 2.50) = .5 - P(0 < Z < 2.50) = .5 - .4938 = .0062$

9.9 a $P(\bar{X} > 1050) = P\left(\frac{\bar{X} - \mu}{\sigma/\sqrt{n}} > \frac{1050 - 1000}{200/\sqrt{100}}\right) = P(Z > 2.50) = .5 - P(0 < Z < 2.50) = .5 - .4938 = .0062$

$$b \ P(\bar{X} < 960) = P\left(\frac{\bar{X} - \mu}{\sigma/\sqrt{n}} < \frac{960 - 1000}{200/\sqrt{100}}\right) = P(Z < -2.00) = .5 - P(0 < Z < 2.00) = .5 - .4772 = .0228$$

$$c \ P(\bar{X} > 1100) = P\left(\frac{\bar{X} - \mu}{\sigma/\sqrt{n}} > \frac{1100 - 1000}{200/\sqrt{100}}\right) = P(Z > 5.00) = 0$$

$$9.10 \ a \ P(49 < \bar{X} < 52) = P\left(\frac{49 - 50}{5/\sqrt{4}} < \frac{\bar{X} - \mu}{\sigma/\sqrt{n}} < \frac{52 - 50}{5/\sqrt{4}}\right) = P(-.40 < Z < .80) \\ = P(0 < Z < .40) + P(0 < Z < .80) = .1554 + .2881 = .4435$$

$$b \ P(49 < \bar{X} < 52) = P\left(\frac{49 - 50}{5/\sqrt{16}} < \frac{\bar{X} - \mu}{\sigma/\sqrt{n}} < \frac{52 - 50}{5/\sqrt{16}}\right) = P(-.80 < Z < 1.60) \\ = P(0 < Z < .80) + P(0 < Z < 1.60) = .2881 + .4452 = .7333$$

$$c \ P(49 < \bar{X} < 52) = P\left(\frac{49 - 50}{5/\sqrt{25}} < \frac{\bar{X} - \mu}{\sigma/\sqrt{n}} < \frac{52 - 50}{5/\sqrt{25}}\right) = P(-1.00 < Z < 2.00) \\ = P(0 < Z < 1.00) + P(0 < Z < 2.00) = .3413 + .4772 = .8185$$

$$9.11 \ a \ P(49 < \bar{X} < 52) = P\left(\frac{49 - 50}{10/\sqrt{4}} < \frac{\bar{X} - \mu}{\sigma/\sqrt{n}} < \frac{52 - 50}{10/\sqrt{4}}\right) = P(-.20 < Z < .40) \\ = P(0 < Z < .20) + P(0 < Z < .40) = .0793 + .1554 = .2347$$

$$b \ P(49 < \bar{X} < 52) = P\left(\frac{49 - 50}{10/\sqrt{16}} < \frac{\bar{X} - \mu}{\sigma/\sqrt{n}} < \frac{52 - 50}{10/\sqrt{16}}\right) = P(-.40 < Z < .80) \\ = P(0 < Z < .40) + P(0 < Z < .80) = .1554 + .2881 = .4435$$

$$c \ P(49 < \bar{X} < 52) = P\left(\frac{49 - 50}{10/\sqrt{25}} < \frac{\bar{X} - \mu}{\sigma/\sqrt{n}} < \frac{52 - 50}{10/\sqrt{25}}\right) = P(-.50 < Z < 1.00) \\ = P(0 < Z < .50) + P(0 < Z < 1.00) = .1915 + .3413 = .5328$$

$$9.12 \ a \ P(49 < \bar{X} < 52) = P\left(\frac{49 - 50}{20/\sqrt{4}} < \frac{\bar{X} - \mu}{\sigma/\sqrt{n}} < \frac{52 - 50}{20/\sqrt{4}}\right) = P(-.10 < Z < .20) \\ = P(0 < Z < .10) + P(0 < Z < .20) = .0398 + .0793 = .1191$$

$$b \ P(49 < \bar{X} < 52) = P\left(\frac{49 - 50}{20/\sqrt{16}} < \frac{\bar{X} - \mu}{\sigma/\sqrt{n}} < \frac{52 - 50}{20/\sqrt{16}}\right) = P(-.20 < Z < .40) \\ = P(0 < Z < .20) + P(0 < Z < .40) = .0793 + .1554 = .2347$$

$$c \ P(49 < \bar{X} < 52) = P\left(\frac{49 - 50}{20/\sqrt{25}} < \frac{\bar{X} - \mu}{\sigma/\sqrt{n}} < \frac{52 - 50}{20/\sqrt{25}}\right) = P(-.25 < Z < .50) \\ = P(0 < Z < .25) + P(0 < Z < .50) = .0987 + .1915 = .2902$$

$$9.13 \text{ a } \sqrt{\frac{N-n}{N-1}} = \sqrt{\frac{1,000-100}{1,000-1}} = .9492$$

$$\text{b } \sqrt{\frac{N-n}{N-1}} = \sqrt{\frac{3,000-100}{3,000-1}} = .9834$$

$$\text{c } \sqrt{\frac{N-n}{N-1}} = \sqrt{\frac{5,000-100}{5,000-1}} = .9900$$

d. The finite population correction factor is approximately 1.

$$9.14 \text{ a } \sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}} \sqrt{\frac{N-n}{N-1}} = \frac{500}{\sqrt{1,000}} \sqrt{\frac{10,000-1,000}{10,000-1}} = 15.00$$

$$\text{b } \sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}} \sqrt{\frac{N-n}{N-1}} = \frac{500}{\sqrt{500}} \sqrt{\frac{10,000-500}{10,000-1}} = 21.80$$

$$\text{c } \sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}} \sqrt{\frac{N-n}{N-1}} = \frac{500}{\sqrt{100}} \sqrt{\frac{10,000-100}{10,000-1}} = 49.75$$

$$9.15 \text{ a } P(X > 168) = P\left(\frac{X-\mu}{\sigma} > \frac{168-163}{5}\right) = P(Z > 1.00) = .5 - P(0 < Z < 1.00) = .5 - .3413 = .1587$$

$$\text{b } P(\bar{X} > 168) = P\left(\frac{\bar{X}-\mu}{\sigma/\sqrt{n}} > \frac{168-163}{5/\sqrt{4}}\right) = P(Z > 2.00) = .5 - P(0 < Z < 2.00) = .5 - .4772 = .0228$$

$$\text{c } P(\bar{X} > 168) = P\left(\frac{\bar{X}-\mu}{\sigma/\sqrt{n}} > \frac{168-163}{2/\sqrt{100}}\right) = P(Z > 10.00) = 0$$

9.16 We can answer part (c) and possibly part (b) depending on how nonnormal the population is.

$$9.17 \text{ a } P(X > 120) = P\left(\frac{X-\mu}{\sigma} > \frac{120-117}{6.1}\right) = P(Z > 0.49) = .5 - P(0 < Z < .49) = .5 - .1879 = .3121$$

$$\text{b } P(\bar{X} > 120) = P\left(\frac{\bar{X}-\mu}{\sigma/\sqrt{n}} > \frac{120-117}{6.1/\sqrt{4}}\right) = P(Z > .98) = .5 - P(0 < Z < .98) = .5 - .3365 = .1635$$

$$\text{c } [P(X > 120)]^4 = [.3121]^4 = .00949$$

$$9.18 \text{ a } P(X > 12) = P\left(\frac{X-\mu}{\sigma} > \frac{12-10}{3}\right) = P(Z > .67) = .5 - P(0 < Z < .67) = .5 - .2486 = .2514$$

$$\begin{aligned} \text{b } P(\bar{X} > 275/25) &= P(\bar{X} > 11) = P\left(\frac{\bar{X}-\mu}{\sigma/\sqrt{n}} > \frac{11-10}{3/\sqrt{25}}\right) = P(Z > 1.67) = .5 - P(0 < Z < 1.67) \\ &= .5 - .4525 = .0475 \end{aligned}$$

$$9.19 \text{ a } P(X > 60) = P\left(\frac{X - \mu}{\sigma} > \frac{60 - 50}{8}\right) = P(Z > 1.25) = .5 - P(0 < Z < 1.25) = .5 - .3944 = .1056$$

$$\text{b } P(\bar{X} > 60) = P\left(\frac{\bar{X} - \mu}{\sigma/\sqrt{n}} > \frac{60 - 50}{8/\sqrt{3}}\right) = P(Z > 2.17) = .5 - P(0 < Z < 2.17) = .5 - .4850 = .0150$$

$$\text{c } [P(X > 60)]^3 = [.1056]^3 = .00118$$

$$9.20 \text{ a } P(X < 75) = P\left(\frac{X - \mu}{\sigma} < \frac{75 - 78}{6}\right) = P(Z < -.50) = .5 - P(0 < Z < .50) = .5 - .1915 = .3085$$

$$\text{b } P(\bar{X} < 75) = P\left(\frac{\bar{X} - \mu}{\sigma/\sqrt{n}} < \frac{75 - 78}{6/\sqrt{50}}\right) = P(Z < -3.54) = .5 - P(0 < Z < 3.54) = .5 - .5 = 0$$

$$9.21 \text{ a } P(X > 6) = P\left(\frac{X - \mu}{\sigma} > \frac{6 - 5}{1.5}\right) = P(Z > .67) = .5 - P(0 < Z < .67) = .5 - .2486 = .2514$$

$$\text{b } P(\bar{X} > 6) = P\left(\frac{\bar{X} - \mu}{\sigma/\sqrt{n}} > \frac{6 - 5}{1.5/\sqrt{5}}\right) = P(Z > 1.49) = .5 - P(0 < Z < 1.49) = .5 - .4319 = .0681$$

$$\text{c } [P(X > 7)]^5 = [.2514]^5 = .00100$$

$$9.22 \text{ } P(\bar{X} > 10,000/16) = P(\bar{X} > 625) = P\left(\frac{\bar{X} - \mu}{\sigma/\sqrt{n}} > \frac{625 - 600}{200/\sqrt{16}}\right) = P(Z > .50) \\ = .5 - P(0 < Z < .50) = .5 - .1915 = .3085$$

$$9.23 \text{ a } P(\bar{X} < 5.97) = P\left(\frac{\bar{X} - \mu}{\sigma/\sqrt{n}} < \frac{5.97 - 6.05}{.18/\sqrt{36}}\right) = P(Z < -2.67) = .5 - P(0 < Z < 2.67) = .5 - .4962 = .0038$$

b It appears to be false.

9.24 The professor needs to know the mean and standard deviation of the population of the weights of elevator users and that the distribution is not extremely nonnormal.

$$9.25 \text{ } P(\bar{X} > 1,140/16) = P(\bar{X} > 71.25) = P\left(\frac{\bar{X} - \mu}{\sigma/\sqrt{n}} > \frac{71.25 - 75}{10/\sqrt{16}}\right) = P(Z > -1.50) \\ = .5 + P(0 < Z < 1.50) = .5 + .4332 = .9332$$

$$9.26 \text{ } P(\text{Total time} > 300) = P(\bar{X} > 300/60) = P(\bar{X} > 5) = P\left(\frac{\bar{X} - \mu}{\sigma/\sqrt{n}} > \frac{5 - 4.8}{1.3/\sqrt{60}}\right) = P(Z > 1.19) \\ = .5 - P(0 < Z < 1.19) = .5 - .3830 = .1170$$

9.27, No because the central limit theorem says that the sample mean is approximately normally distributed.

$$9.28 P(\text{Total number of faxes} > 1500) = P(\bar{X} > 1500/5) = P(\bar{X} > 300) = P\left(\frac{\bar{X} - \mu}{\sigma/\sqrt{n}} > \frac{300 - 275}{75/\sqrt{5}}\right)$$

$$= P(Z > .75) = .5 - P(0 < Z < .75) = .5 - .2734 = .2266$$

$$9.29 P(\text{Total number of cups} > 225) = P(\bar{X} > 225/125) = P(\bar{X} > 1.80) = P\left(\frac{\bar{X} - \mu}{\sigma/\sqrt{n}} > \frac{1.80 - 1.7}{.5/\sqrt{125}}\right)$$

$$= P(Z > 2.24) = .5 - P(0 < Z < 2.24) = .5 - .4875 = .0125$$

$$9.30a P(\hat{P} > .60) = P\left(\frac{\hat{P} - p}{\sqrt{p(1-p)/n}} > \frac{.60 - .5}{\sqrt{(.5)(1-.5)/300}}\right) = P(Z > 3.46) = 0$$

$$b. P(\hat{P} > .60) = P\left(\frac{\hat{P} - p}{\sqrt{p(1-p)/n}} > \frac{.60 - .55}{\sqrt{(.55)(1-.55)/300}}\right) = P(Z > 1.74) = .5 - P(0 < Z < 1.74) = .5 - .4591$$

$$= .0409$$

$$c. P(\hat{P} > .60) = P\left(\frac{\hat{P} - p}{\sqrt{p(1-p)/n}} > \frac{.60 - .6}{\sqrt{(.6)(1-.6)/300}}\right) = P(Z > 0) = .5$$

$$9.31a P(\hat{P} < .22) = P\left(\frac{\hat{P} - p}{\sqrt{p(1-p)/n}} > \frac{.22 - .25}{\sqrt{(.25)(1-.25)/500}}\right) = P(Z < -1.55) = .5 - P(0 < Z < 1.55)$$

$$= .5 - .4394 = .0606$$

$$b. P(\hat{P} < .22) = P\left(\frac{\hat{P} - p}{\sqrt{p(1-p)/n}} > \frac{.22 - .25}{\sqrt{(.25)(1-.25)/800}}\right) = P(Z < -1.96) = .5 - P(0 < Z < 1.96) = .5 - .4750$$

$$= .0250$$

$$c. P(\hat{P} < .22) = P\left(\frac{\hat{P} - p}{\sqrt{p(1-p)/n}} > \frac{.22 - .25}{\sqrt{(.25)(1-.25)/1000}}\right) = P(Z < -2.19) = .5 - P(0 < Z < 2.19) = .5 - .4857$$

$$= .0143$$

$$9.32 P(\hat{P} < .75) = P\left(\frac{\hat{P} - p}{\sqrt{p(1-p)/n}} > \frac{.75 - .80}{\sqrt{(.80)(1-.80)/100}}\right) = P(Z < -1.25) = .5 - P(0 < Z < 1.25)$$

$$= .5 - .3944 = .1056$$

$$9.33 P(\hat{P} > .35) = P\left(\frac{\hat{P} - p}{\sqrt{p(1-p)/n}} > \frac{.35 - .40}{\sqrt{(.40)(1-.40)/60}}\right) = P(Z > -.79) = .5 + P(0 < Z < .79) = .5 + .2852$$

$$= .7852$$

$$9.34 \text{ P}(\hat{P} < .49) = \text{P}\left(\frac{\hat{P} - p}{\sqrt{p(1-p)/n}} < \frac{.49 - .52}{\sqrt{(.52)(1-.52)/500}}\right) = \text{P}(Z < -1.34) = .5 - \text{P}(0 < Z < 1.34) \\ = .5 - .4099 = .0901$$

$$9.35 \text{ P}(\hat{P} > .05) = \text{P}\left(\frac{\hat{P} - p}{\sqrt{p(1-p)/n}} > \frac{.05 - .03}{\sqrt{(.03)(1-.03)/800}}\right) = \text{P}(Z > 3.32) = 0;$$

The defective appears to be larger than 3%.

$$9.36 \text{ a P}(\hat{P} < .50) = \text{P}\left(\frac{\hat{P} - p}{\sqrt{p(1-p)/n}} < \frac{.50 - .52}{\sqrt{(.52)(1-.52)/400}}\right) = \text{P}(Z < -.80) = .5 - \text{P}(0 < Z < .80) \\ = .5 - .2881 = .2119; \text{ the claim may be true.}$$

$$\text{b P}(\hat{P} < .50) = \text{P}\left(\frac{\hat{P} - p}{\sqrt{p(1-p)/n}} < \frac{.50 - .52}{\sqrt{(.52)(1-.52)/1,000}}\right) = \text{P}(Z < -1.27) = .5 - \text{P}(0 < Z < 1.27) \\ = .5 - .3980 = .1020; \text{ the claim may be true.}$$

$$9.37 \text{ P}(\hat{P} > .20) = \text{P}\left(\frac{\hat{P} - p}{\sqrt{p(1-p)/n}} > \frac{.20 - .24}{\sqrt{(.24)(1-.24)/100}}\right) = \text{P}(Z > -.94) \\ = .5 + \text{P}(0 < Z < .94) = .5 + .3264 = .8264$$

$$9.38 \text{ P}(\hat{P} > .05) = \text{P}\left(\frac{\hat{P} - p}{\sqrt{p(1-p)/n}} > \frac{.05 - .03}{\sqrt{(.03)(1-.03)/400}}\right) = \text{P}(Z > 2.34) = .5 - \text{P}(0 < Z < 2.34) = .5 - .4904 \\ = .0096; \text{ the commercial appears to be dishonest}$$

$$9.39 \text{ P}(\hat{P} > .22) = \text{P}\left(\frac{\hat{P} - p}{\sqrt{p(1-p)/n}} > \frac{.22 - .20}{\sqrt{(.20)(1-.20)/1,000}}\right) = \text{P}(Z > 1.58) = .5 - \text{P}(0 < Z < 1.58) \\ = .5 - .4429 = .0571$$

$$9.40 \text{ a P}(\hat{P} < .45) = \text{P}\left(\frac{\hat{P} - p}{\sqrt{p(1-p)/n}} < \frac{.45 - .50}{\sqrt{(.50)(1-.50)/600}}\right) = \text{P}(Z < -2.45) = .5 - \text{P}(0 < Z < 2.45) \\ = .5 - .4929 = .0071$$

b The claim appears to be false.

$$9.41 \ P(\hat{P} < .55) = P\left(\frac{\hat{P}-p}{\sqrt{p(1-p)/n}} < \frac{.55-.60}{\sqrt{(.60)(1-.60)/480}}\right) = P(Z < -2.24) = .5 - P(0 < Z < 2.24) \\ = .5 - .4875 = .0125$$

$$9.42 \ P(\hat{P} < .75) = P\left(\frac{\hat{P}-p}{\sqrt{p(1-p)/n}} < \frac{.75-.80}{\sqrt{(.80)(1-.80)/350}}\right) = P(Z < -2.34) \\ = .5 - P(0 < Z < 2.34) = .5 - .4904 = .0096$$

$$9.43 \ P(\hat{P} > .28) = P\left(\frac{\hat{P}-p}{\sqrt{p(1-p)/n}} > \frac{.28-.25}{\sqrt{(.25)(1-.25)/1200}}\right) = P(Z > 2.40) \\ = .5 - P(0 < Z < 2.40) = .5 - .4918 = .0082$$

9.44 The claim appears to be false.

$$9.45 \ P(\bar{X}_1 - \bar{X}_2 > 25) = P\left(\frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}} > \frac{25 - (280 - 270)}{\sqrt{\frac{25^2}{10} + \frac{30^2}{10}}}\right) = P(Z > 1.21) = .5 - P(0 < Z < 1.21) \\ = .5 - .3869 = .1131$$

$$9.46 \ P(\bar{X}_1 - \bar{X}_2 > 25) = P\left(\frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}} > \frac{25 - (280 - 270)}{\sqrt{\frac{25^2}{50} + \frac{30^2}{50}}}\right) = P(Z > 2.72) = .5 - P(0 < Z < 2.72) \\ = .5 - .4967 = .0033$$

$$9.47 \ P(\bar{X}_1 - \bar{X}_2 > 25) = P\left(\frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}} > \frac{25 - (280 - 270)}{\sqrt{\frac{25^2}{100} + \frac{30^2}{100}}}\right) = P(Z > 3.84) = 0$$

$$9.48 \ P(\bar{X}_1 - \bar{X}_2 > 0) = P\left(\frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}} > \frac{0 - (40 - 38)}{\sqrt{\frac{6^2}{25} + \frac{8^2}{25}}}\right) = P(Z > -1.00) = .5 + P(0 < Z < 1.00) \\ = .5 + .3413 = .8413$$

$$9.49 \ P(\bar{X}_1 - \bar{X}_2 > 0) = P\left(\frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}} > \frac{0 - (40 - 38)}{\sqrt{\frac{12^2}{25} + \frac{16^2}{25}}}\right) = P(Z > -.50) = .5 + P(0 < Z < .50)$$

$$= .5 + .1915 = .6915$$

$$9.50 \ P(\bar{X}_1 - \bar{X}_2 > 0) = P\left(\frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}} > \frac{0 - (140 - 138)}{\sqrt{\frac{6^2}{25} + \frac{8^2}{25}}}\right) = P(Z > -1.00) = .5 + P(0 < Z < 1.00)$$

$$= .5 + .3413 = .8413$$

$$9.51 \ P(\bar{X}_1 - \bar{X}_2 > 0) = P\left(\frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}} > \frac{0 - (75 - 65)}{\sqrt{\frac{20^2}{5} + \frac{21^2}{5}}}\right) = P(Z > -.77)$$

$$= .5 + P(0 < Z < .77) = .5 + .2794 = .7794$$

$$9.52 \ P(\bar{X}_1 - \bar{X}_2 > 0) = P\left(\frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}} > \frac{0 - (73 - 77)}{\sqrt{\frac{12^2}{4} + \frac{10^2}{4}}}\right) = P(Z > .51) = .5 - P(0 < Z < .51)$$

$$= .5 - .1950 = .3050$$

$$9.53 \ P(\bar{X}_1 - \bar{X}_2 > 0) = P\left(\frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}} > \frac{0 - (18 - 15)}{\sqrt{\frac{3^2}{10} + \frac{3^2}{10}}}\right) = P(Z > -2.24) = .5 + P(0 < Z < 2.24)$$

$$= .5 + .4875 = .9875$$

$$9.54 \ P(\bar{X}_1 - \bar{X}_2 < 0) = P\left(\frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}} < \frac{0 - (10 - 15)}{\sqrt{\frac{3^2}{25} + \frac{3^2}{25}}}\right) = P(Z < 5.89) = 1$$

