

Chapter 6

6.1 a Relative frequency approach

b If the conditions today repeat themselves an infinite number of days rain will fall on 10% of the next days.

6.2 a Subjective approach

b If all the teams in major league baseball have exactly the same players the New York Yankees will win 25% of all World Series.

6.3 a {a is correct, b is correct, c is correct, d is correct, e is correct}

b $P(\text{a is correct}) = P(\text{b is correct}) = P(\text{c is correct}) = P(\text{d is correct}) = P(\text{e is correct}) = .2$

c Classical approach

d In the long run all answers are equally likely to be correct.

6.4 a Subjective approach

b The Dow Jones Industrial Index will increase on 60% of the days if economic conditions remain unchanged.

6.5 a $P(\text{even number}) = P(2) + P(4) + P(6) = 1/6 + 1/6 + 1/6 = 3/6 = 1/2$

b $P(\text{number less than or equal to 4}) = P(1) + P(2) + P(3) + P(4) = 1/6 + 1/6 + 1/6 + 1/6 = 4/6 = 2/3$

c $P(\text{number greater than or equal to 5}) = P(5) + P(6) = 1/6 + 1/6 = 2/6 = 1/3$

6.6 {Adams wins, Brown wins, Collins wins, Dalton wins}

6.7a $P(\text{Adams loses}) = P(\text{Brown wins}) + P(\text{Collins wins}) + P(\text{Dalton wins}) = .09 + .27 + .22 = .58$

b $P(\text{either Brown or Dalton wins}) = P(\text{Brown wins}) + P(\text{Dalton wins}) = .09 + .22 = .31$

c $P(\text{either Adams, Brown, or Collins wins}) = P(\text{Adams wins}) + P(\text{Brown wins}) + P(\text{Collins wins})$
 $= .42 + .09 + .27 = .78$

6.8 a {0, 1, 2, 3, 4, 5}

b {4, 5}

c $P(5) = .10$

d $P(2, 3, \text{ or } 4) = P(2) + P(3) + P(4) = .26 + .21 + .18 = .65$

e $P(6) = 0$

6.9 {Contractor 1 wins, Contractor 2 wins, Contractor 3 wins}

6.10 $P(\text{Contractor 1 wins}) = 2/6, P(\text{Contractor 2 wins}) = 3/6, P(\text{Contractor 3 wins}) = 1/6$

6.11 a {Shopper pays cash, shopper pays by credit card, shopper pays by debit card}

b $P(\text{Shopper pays cash}) = .30$, $P(\text{Shopper pays by credit card}) = .60$, $P(\text{Shopper pays by debit card}) = .10$

c Relative frequency approach

6.12 a $P(\text{shopper does not use credit card}) = P(\text{shopper pays cash}) + P(\text{shopper pays by debit card})$

$$= .30 + .10 = .40$$

b $P(\text{shopper pays cash or uses a credit card}) = P(\text{shopper pays cash}) + P(\text{shopper pays by credit card})$

$$= .30 + .60 = .90$$

6.13 {single, divorced, widowed}

6.14 a $P(\text{single}) = .15$, $P(\text{married}) = .50$, $P(\text{divorced}) = .25$, $P(\text{widowed}) = .10$

b Relative frequency approach

6.15 a $P(\text{single}) = .15$

b $P(\text{adult is not divorced}) = P(\text{single}) + P(\text{married}) + P(\text{widowed}) = .15 + .50 + .10 = .75$

c $P(\text{adult is either widowed or divorced}) = P(\text{divorced}) + P(\text{widowed}) = .25 + .10 = .35$

6.16 $P(A_1) = .4 + .2 = .6$, $P(A_2) = .3 + .1 = .4$. $P(B_1) = .4 + .3 = .7$, $P(B_2) = .2 + .1 = .3$.

6.17 $P(A_1) = .1 + .2 = .3$, $P(A_2) = .3 + .1 = .4$, $P(A_3) = .2 + .1 = .3$.

$P(B_1) = .1 + .3 + .2 = .6$, $P(B_2) = .2 + .1 + .1 = .4$.

6.18 a
$$P(A_1 | B_1) = \frac{P(A_1 \text{ and } B_1)}{P(B_1)} = \frac{.4}{.7} = .57$$

b
$$P(A_2 | B_1) = \frac{P(A_2 \text{ and } B_1)}{P(B_1)} = \frac{.3}{.7} = .43$$

c Yes. It is not a coincidence. Given B_1 the events A_1 and A_2 constitute the entire sample space.

6.19 a
$$P(A_1 | B_2) = \frac{P(A_1 \text{ and } B_2)}{P(B_2)} = \frac{.2}{.3} = .67$$

b
$$P(B_2 | A_1) = \frac{P(A_1 \text{ and } B_2)}{P(A_1)} = \frac{.2}{.6} = .33$$

c One of the conditional probabilities would be greater than 1, which is not possible.

6.20 The events are not independent because $P(A_1 | B_2) \neq P(A_1)$.

$$6.21 \text{ a } P(A_1 \text{ or } B_1) = P(A_1) + P(B_1) - P(A_1 \text{ and } B_1) = .6 + .7 - .4 = .9$$

$$\text{b } P(A_1 \text{ or } B_2) = P(A_1) + P(B_2) - P(A_1 \text{ and } B_2) = .6 + .3 - .2 = .7$$

$$\text{c } P(A_1 \text{ or } A_2) = P(A_1) + P(A_2) = .6 + .4 = 1$$

$$6.22 \text{ a } P(A_1 | B_1) = \frac{P(A_1 \text{ and } B_1)}{P(B_1)} = \frac{.20}{.20 + .15} = .571; P(A_1) = .20 + .60 = .80; \text{ the events are dependent.}$$

$$6.23 \text{ a } P(A_1 | B_1) = \frac{P(A_1 \text{ and } B_1)}{P(B_1)} = \frac{.20}{.20 + .60} = .25; P(A_1) = .20 + .05 = .25; \text{ the events are independent.}$$

$$6.24 \text{ a } P(A_1) = .20 + .25 = .45, P(A_2) = .15 + .25 = .40, P(A_3) = .10 + .05 = .15.$$

$$P(B_1) = .20 + .15 + .10 = .45, P(B_2) = .25 + .25 + .05 = .55.$$

$$6.25 \text{ a } P(A_2 | B_2) = \frac{P(A_2 \text{ and } B_2)}{P(B_2)} = \frac{.25}{.55} = .455$$

$$\text{b } P(B_2 | A_2) = \frac{P(A_2 \text{ and } B_2)}{P(A_2)} = \frac{.25}{.40} = .625$$

$$\text{c } P(B_1 | A_2) = \frac{P(A_2 \text{ and } B_1)}{P(A_2)} = \frac{.15}{.40} = .375$$

$$6.26 \text{ a } P(A_1 \text{ or } A_2) = P(A_1) + P(A_2) = .45 + .40 = .85$$

$$\text{b } P(A_2 \text{ or } B_2) = P(A_2) + P(B_2) - P(A_2 \text{ and } B_2) = .40 + .55 - .25 = .70$$

$$\text{c } P(A_3 \text{ or } B_1) = P(A_3) + P(B_1) - P(A_3 \text{ and } B_1) = .15 + .45 - .10 = .50$$

$$6.27 \text{ a } P(\text{debit card}) = .04 + .18 + .14 = .36$$

$$\text{b } P(\text{over } \$100 | \text{credit card}) = \frac{P(\text{credit card and over } \$100)}{P(\text{credit card})} = \frac{.23}{.03 + .21 + .23} = .49$$

$$\text{c } P(\text{credit card or debit card}) = P(\text{credit card}) + P(\text{debit card}) = .47 + .36 = .83$$

$$6.28 \text{ a } P(\text{promoted} | \text{female}) = \frac{P(\text{promoted and female})}{P(\text{female})} = \frac{.05}{.05 + .12} = .294$$

$$\text{b } P(\text{promoted} | \text{male}) = \frac{P(\text{promoted and male})}{P(\text{male})} = \frac{.15}{.15 + .68} = .181$$

c Yes, because promotion and gender are not independent events.

6.29 a $P(\text{voted}) = .25 + .18 = .43$

b $P(\text{voted} | \text{female}) = \frac{P(\text{voted and female})}{P(\text{female})} = \frac{.25}{.25 + .33} = .431$, $P(\text{voted}) = .43$, Subject to rounding the

events are independent.

6.30 a $P(\text{He is a smoker}) = .10 + .21 = .31$

b $P(\text{He does not have lung disease}) = .21 + .66 = .87$

c $P(\text{He has lung disease} | \text{he is a smoker}) = \frac{P(\text{he has lung disease and he is a smoker})}{P(\text{he is a smoker})} = \frac{.10}{.31} = .323$

d $P(\text{He has lung disease} | \text{he does not smoke}) = \frac{P(\text{he has lung disease and he does not smoke})}{P(\text{he does not smoke})} = \frac{.03}{.69} = .044$

6.31 The events are dependent because $P(\text{he has lung disease}) = .13$, $P(\text{he has lung disease} | \text{he is a smoker}) = .323$

6.32 a $P(\text{manual} | \text{math-stats}) = \frac{P(\text{manual and math-stats})}{P(\text{math-stats})} = \frac{.23}{.23 + .36} = .390$

b $P(\text{computer}) = .36 + .30 = .66$

c No, because $P(\text{manual}) = .23 + .11 = .34$, which is not equal to $P(\text{manual} | \text{math-stats})$.

6.33 a $P(\text{customer will return and good rating}) = .35$

b $P(\text{good rating} | \text{will return}) = \frac{P(\text{good rating and will return})}{P(\text{will return})} = \frac{.35}{.02 + .08 + .35 + .20} = \frac{.35}{.65} = .538$

c $P(\text{will return} | \text{good rating}) = \frac{P(\text{good rating and will return})}{P(\text{good rating})} = \frac{.35}{.35 + .14} = \frac{.35}{.49} = .714$

d (a) is the joint probability and (b) and (c) are conditional probabilities

6.34 a $P(\text{ask} | \text{male}) = \frac{P(\text{ask and male})}{P(\text{male})} = \frac{.12}{.23 + .12 + .15} = \frac{.12}{.50} = .24$

b $P(\text{consult a map}) = .23 + .14 = .37$

c No, because $P(\text{consult map} | \text{male}) = \frac{P(\text{consult a map and male})}{P(\text{male})} = \frac{.23}{.23 + .12 + .15} = \frac{.23}{.50} = .46$, which is

not equal to $P(\text{consult map})$

6.35 a $P(\text{ulcer}) = .03 + .03 + .03 + .04 = .13$

$$b \ P(\text{ulcer} \mid \text{none}) = \frac{P(\text{ulcer and none})}{P(\text{none})} = \frac{.03}{.03 + .20} = \frac{.03}{.23} = .130$$

$$c \ P(\text{none} \mid \text{ulcer}) = \frac{P(\text{ulcer and none})}{P(\text{ulcer})} = \frac{.03}{.03 + .03 + .03 + .04} = \frac{.03}{.13} = .231$$

$$d \ P(\text{two} \mid \text{no ulcer}) = \frac{P(\text{no ulcer and two})}{P(\text{no ulcer})} = \frac{.32}{.20 + .19 + .32 + .16} = \frac{.32}{.87} = .368$$

$$6.36 \ a \ P(\text{remember}) = .12 + .18 = .30$$

$$b \ P(\text{remember} \mid \text{violent}) = \frac{P(\text{remember and violent})}{P(\text{violent})} = \frac{.12}{.12 + .38} = \frac{.12}{.50} = .24$$

c Yes, the events are dependent.

$$6.37 \ a \ P(\text{above average} \mid \text{murderer}) = \frac{P(\text{above average and murderer})}{P(\text{murderer})} = \frac{.27}{.27 + .21} = \frac{.27}{.48} = .563$$

b No, because $P(\text{above average}) = .27 + .24 = .51$, which is not equal to $P(\text{above average testosterone} \mid \text{murderer})$.

$$6.38 \ a \ P(\text{uses a spreadsheet}) = .311 + .312 = .623$$

$$b \ P(\text{uses a spreadsheet} \mid \text{male}) = \frac{P(\text{uses a spreadsheet and male})}{P(\text{male})} = \frac{.312}{.312 + .168} = \frac{.312}{.480} = .650$$

$$c \ b \ P(\text{female} \mid \text{uses a spreadsheet}) = \frac{P(\text{uses a spreadsheet and female})}{P(\text{uses a spreadsheet})} = \frac{.311}{.311 + .209} = \frac{.311}{.520} = .598$$

6.39 No, because $P(\text{uses a spreadsheet}) \neq P(\text{uses a spreadsheet} \mid \text{male})$

$$6.40 \ a \ P(\text{under 20}) = .2307 + .0993 + .5009 = .8309$$

$$b \ P(\text{retail}) = .5009 + .0876 + .0113 = .5998$$

$$c \ P(20 \text{ to } 99 \mid \text{construction}) = \frac{P(20 \text{ to } 99 \text{ and construction})}{P(\text{construction})} = \frac{.0189}{.2307 + .0189 + .0019} = \frac{.0189}{.2515} = .0751$$

$$6.41 \ a \ P(\text{provided by employer}) = .166 + .195 + .230 = .591$$

b $P(\text{provided by employer} \mid \text{professional/technical}) =$

$$\frac{P(\text{provided by employer and professional / technical})}{P(\text{professional / technical})} = \frac{.166}{.166 + .094} = \frac{.166}{.260} = .638$$

$$c \ \frac{P(\text{provided by employer and blue - collar / services})}{P(\text{blue - collar / services})} = \frac{.230}{.230 + .180} = \frac{.230}{.410} = .561$$

$$6.42 \text{ a } P(\text{new} \mid \text{overdue}) = \frac{P(\text{new and overdue})}{P(\text{overdue})} = \frac{.08}{.08 + .50} = \frac{.08}{.58} = .138$$

$$\text{b } P(\text{overdue} \mid \text{new}) = \frac{P(\text{new and overdue})}{P(\text{new})} = \frac{.08}{.08 + .13} = \frac{.08}{.21} = .381$$

c Yes, because $P(\text{new}) = .21 \neq P(\text{new} \mid \text{overdue})$

$$6.43 \text{ P}(\text{purchase} \mid \text{see ad}) = \frac{P(\text{purchase and see ad})}{P(\text{see ad})} = \frac{.18}{.18 + .42} = \frac{.18}{.60} = .30; \text{ P}(\text{purchase} \mid \text{do not see ad}) =$$

$$\frac{P(\text{purchase and do not see ad})}{P(\text{do not see ad})} = \frac{.12}{.12 + .28} = \frac{.12}{.40} = .30; \text{ the ads are not effective}$$

6.44 a $P(\text{unemployed} \mid \text{high school graduate}) =$

$$\frac{P(\text{unemployed and high school graduate})}{P(\text{high school graduate})} = \frac{.0128}{.3108 + .0128} = \frac{.0128}{.3236} = .0396$$

$$\text{b } P(\text{employed}) = .0975 + .3108 + .1785 + .0849 + .1959 + .0975 = .9651$$

c $P(\text{advanced degree} \mid \text{unemployed}) =$

$$\frac{P(\text{advanced degree and unemployed})}{P(\text{unemployed})} = \frac{.0015}{.0080 + .0128 + .0062 + .0023 + .0041 + .0015} = \frac{.0015}{.0349} = .0430$$

$$\text{d } P(\text{not a high school graduate}) = .0975 + .0080 = .1055$$

$$6.45 \text{ a } P(\text{fully repaid}) = .17 + .66 = .83$$

$$\text{b } P(\text{fully repaid} \mid \text{under 400}) = \frac{P(\text{fully repaid and under 400})}{P(\text{under 400})} = \frac{.17}{.17 + .13} = \frac{.17}{.30} = .567$$

$$\text{c } P(\text{fully repaid} \mid \text{400 or more}) = \frac{P(\text{fully repaid and 400 or more})}{P(\text{400 or more})} = \frac{.66}{.66 + .04} = \frac{.66}{.70} = .943$$

d No, because $P(\text{fully repaid}) \neq P(\text{fully repaid} \mid \text{under 400})$

6.46 a $P(\text{bachelor's degree} \mid \text{west})$

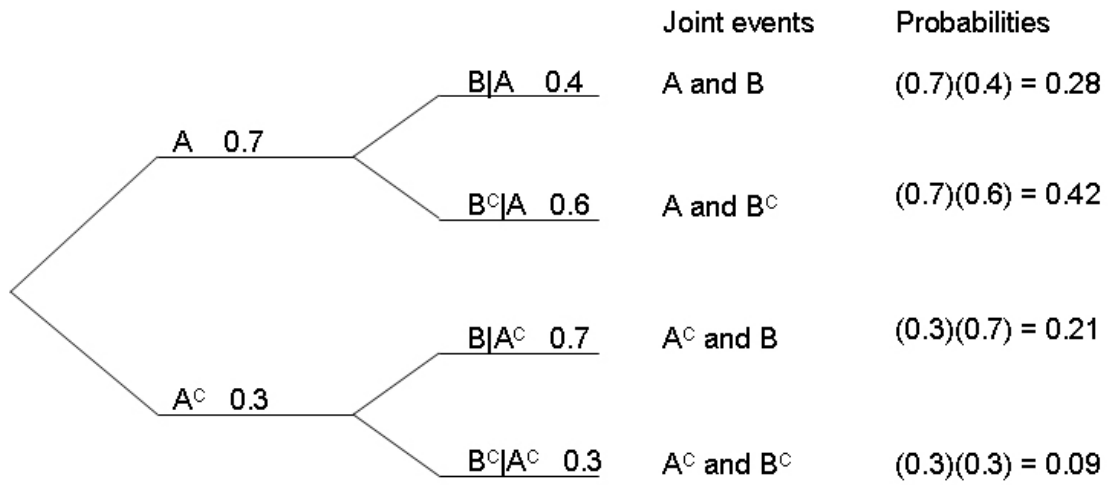
$$= \frac{P(\text{bachelor's degree and west})}{P(\text{west})} = \frac{.0418}{.0359 + .0608 + .0456 + .0181 + .0418 + .0180} = \frac{.0418}{.2202} = .1898$$

b $P(\text{northwest} \mid \text{high school graduate})$

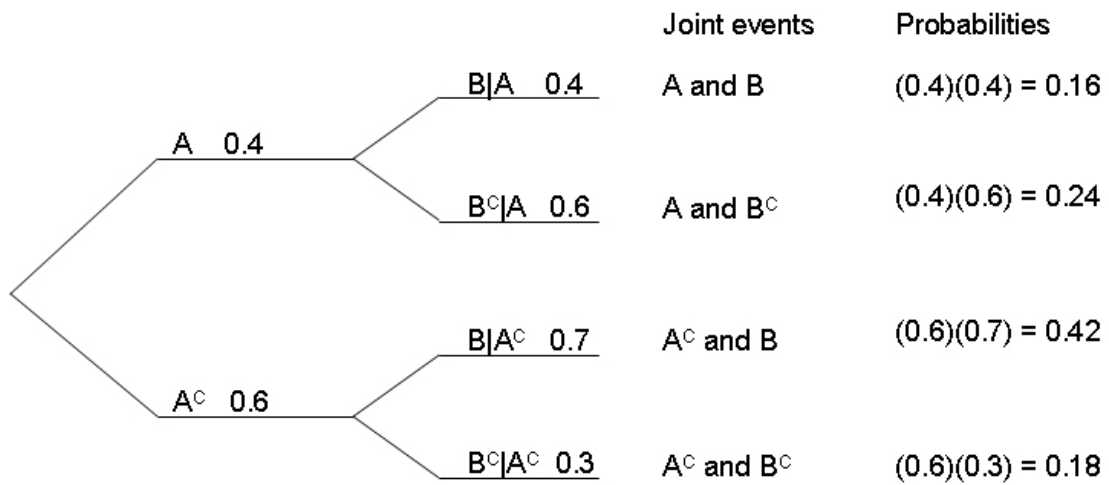
$$= \frac{P(\text{northwest and high school graduate})}{P(\text{high school graduate})} = \frac{.0711}{.0711 + .0843 + .1174 + .0608} = \frac{.0711}{.3336} = .2131$$

$$\text{c } P(\text{south}) = .0683 + .1174 + .0605 + .0248 + .0559 + .0269 = .3538$$

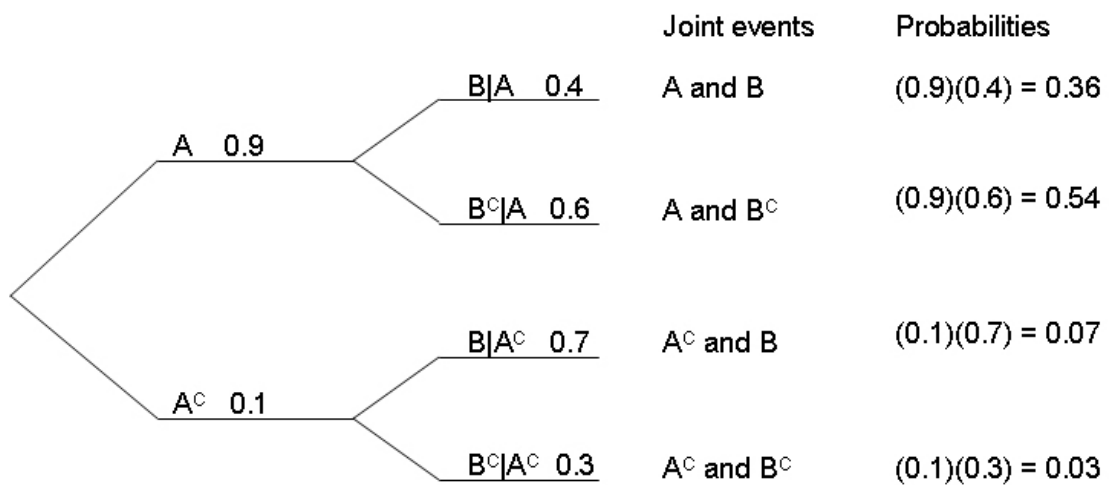
6.47



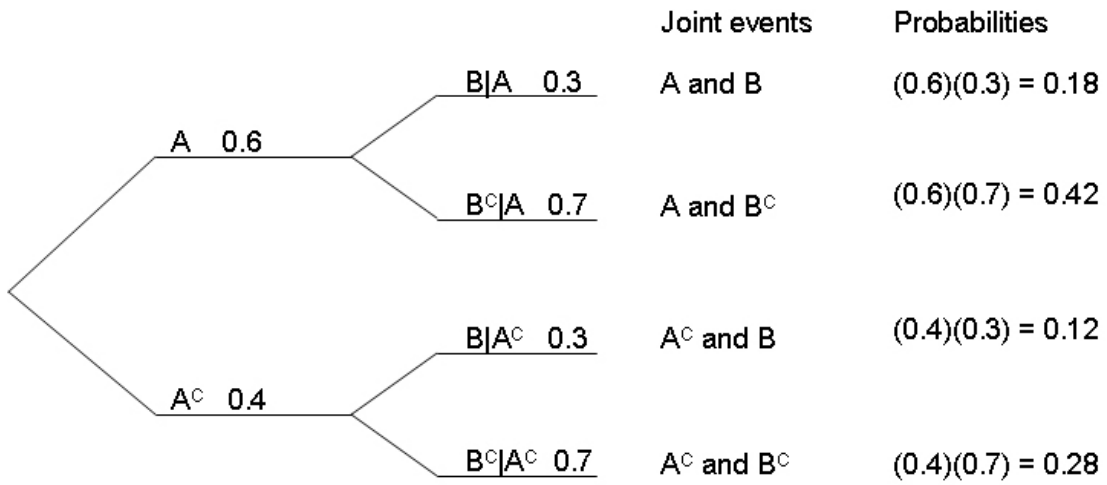
6.48



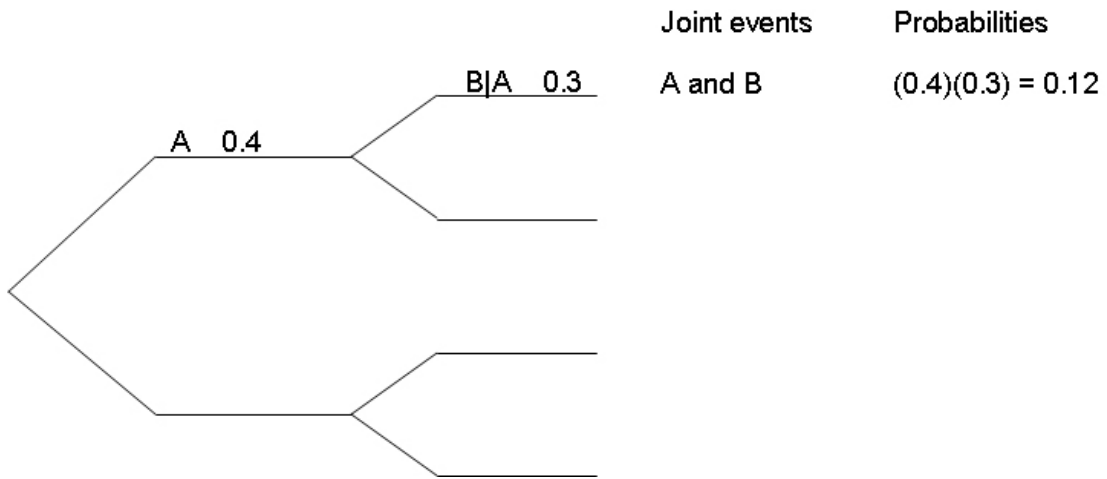
6.49



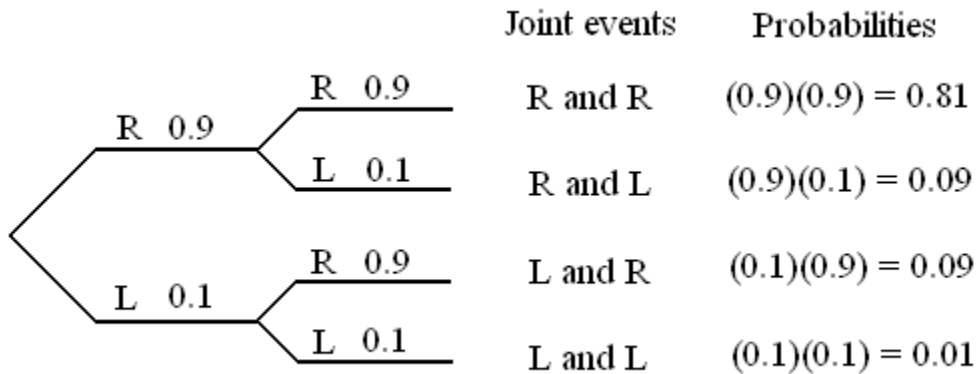
6.50



6.51



6.52



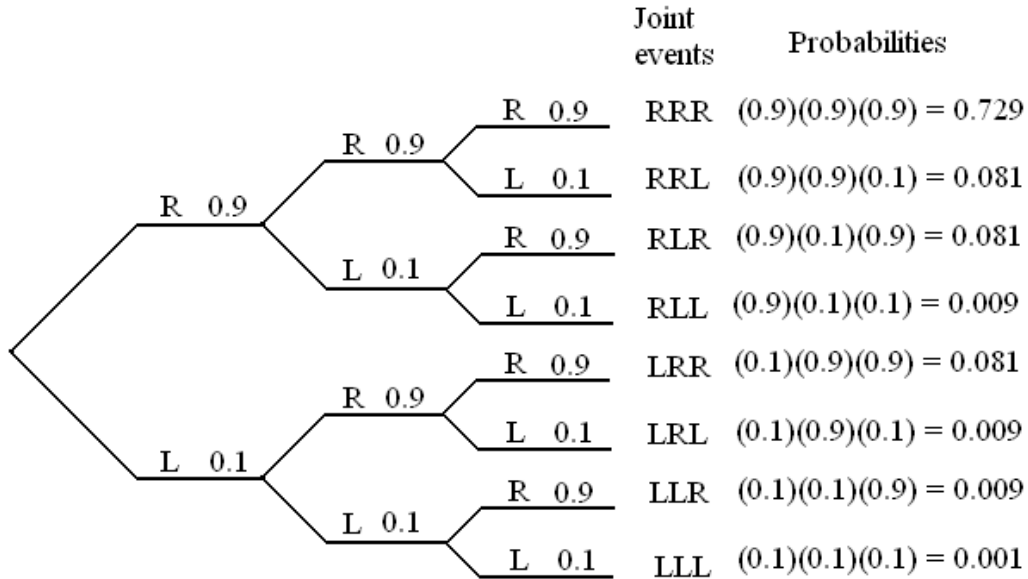
a $P(R \text{ and } R) = .81$

b $P(L \text{ and } L) = .01$

c $P(R \text{ and } L) + P(L \text{ and } R) = .09 + .09 = .18$

d $P(R \text{ and } L) + P(L \text{ and } R) + P(R \text{ and } R) = .09 + .09 + .81 = .99$

6.53 a & b



- c
- | | |
|-----------------|---|
| 0 right-handers | 1 |
| 1 right-hander | 3 |
| 2 right-handers | 3 |
| 3 right-handers | 1 |

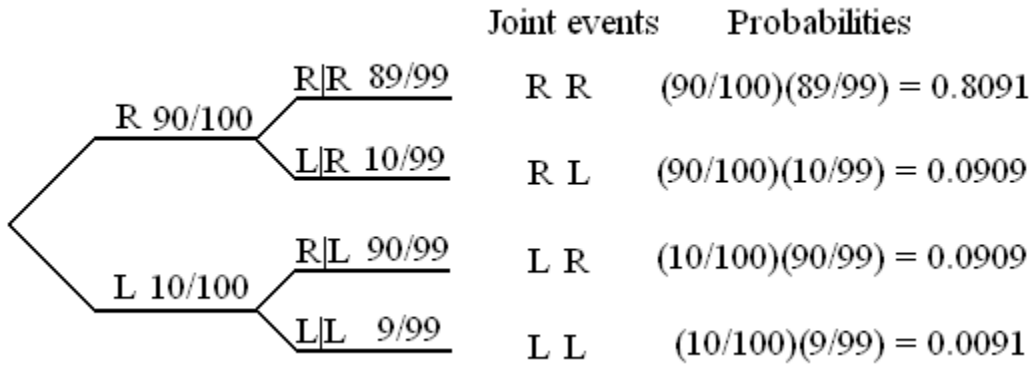
d $P(0 \text{ right-handers}) = .001$

$P(1 \text{ right-hander}) = 3(.009) = .027$

$P(2 \text{ right-handers}) = 3(.081) = .243$

$P(3 \text{ right-handers}) = .729$

6.54a



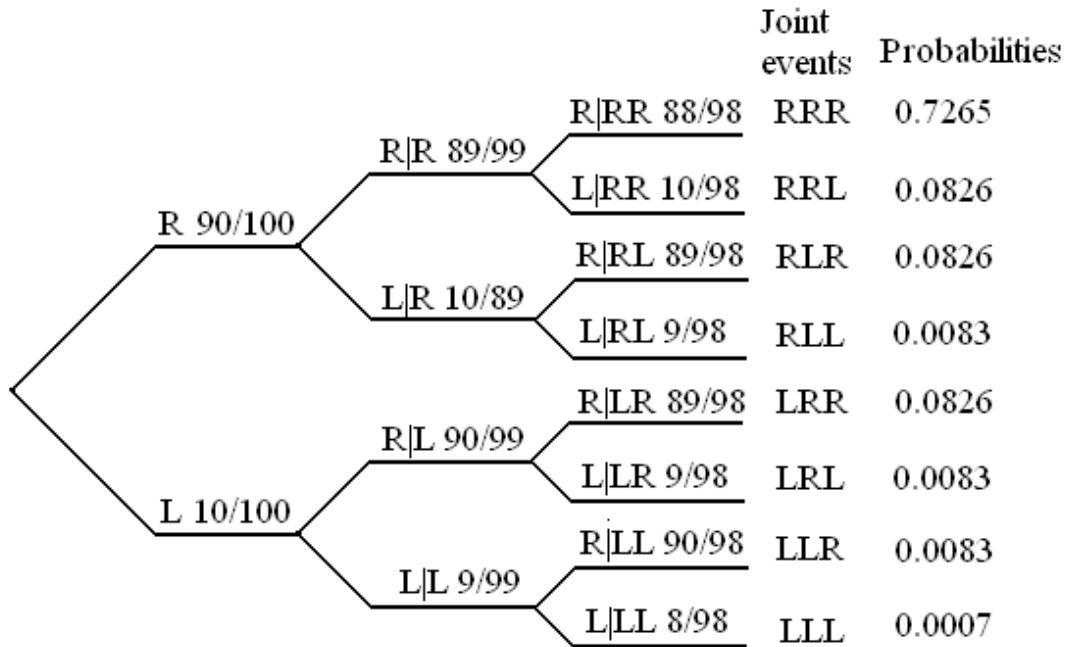
b $P(RR) = .8091$

c $P(LL) = .0091$

d $P(RL) + P(LR) = .0909 + .0909 = .1818$

e $P(RL) + P(LR) + P(RR) = .0909 + .0909 + .8091 = .9909$

6.55a



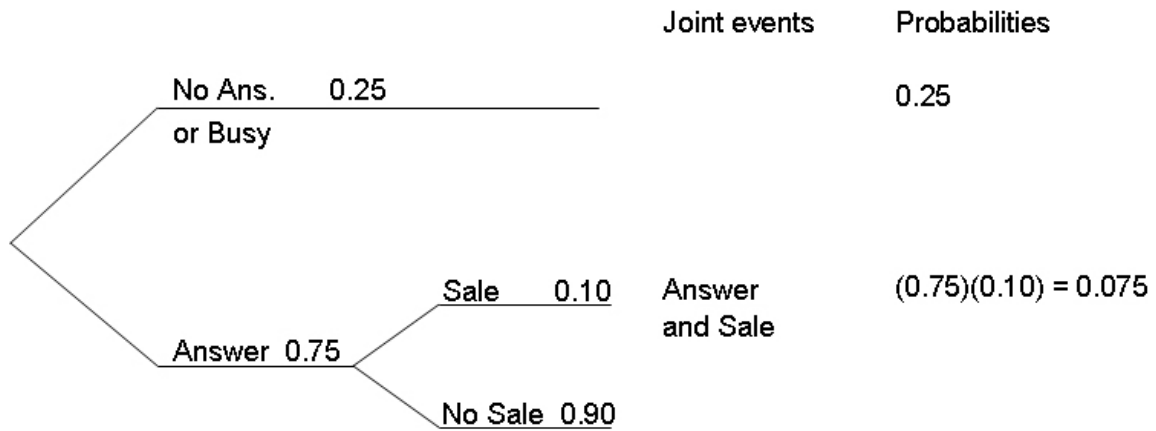
$P(0 \text{ right-handers}) = (10/100)(9/99)(8/98) = .0007$

$P(1 \text{ right-hander}) = 3(90/100)(10/99)(9/98) = .0249$

$P(2 \text{ right-handers}) = 3(90/100)(89/99)(10/98) = .2478$

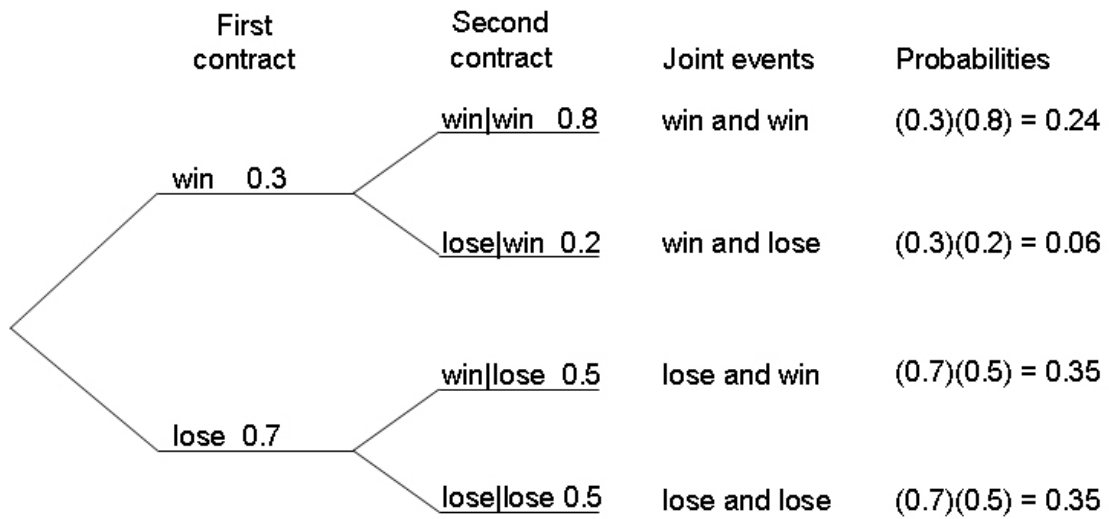
$P(3 \text{ right-handers}) = (90/100)(89/99)(88/98) = .7265$

6.56



$P(\text{sale}) = .075$

6.57

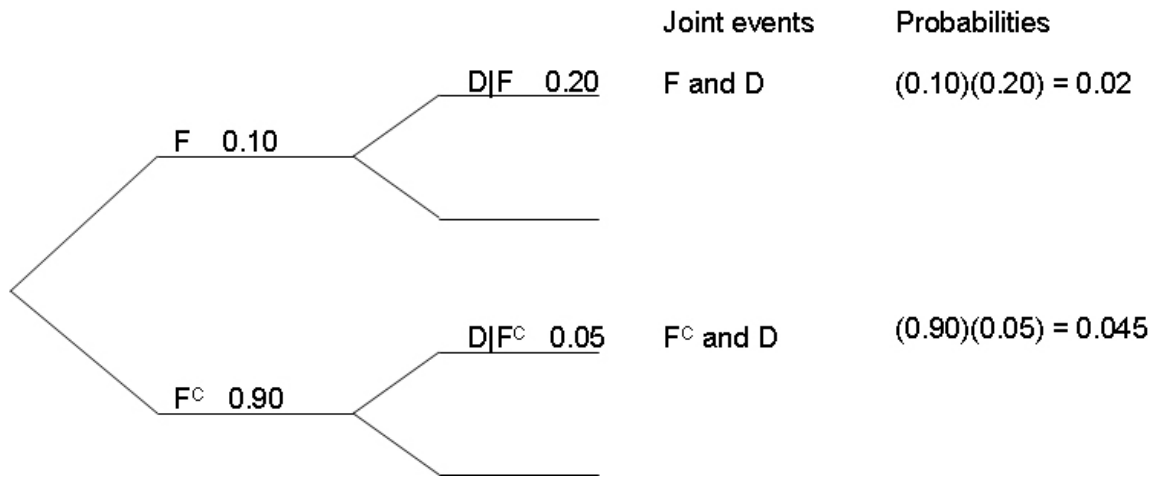


a $P(\text{win both}) = .24$

b $P(\text{lose both}) = .35$

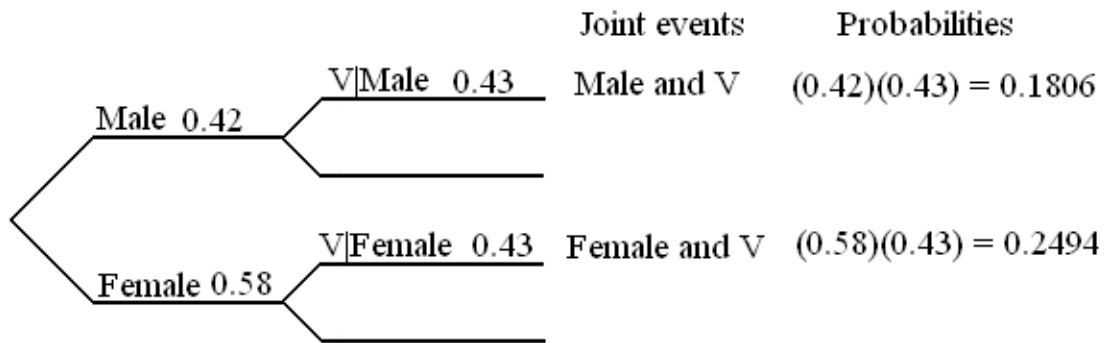
c $P(\text{win only one}) = .06 + .35 = .41$

6.58



$P(D) = .02 + .045 = .065$

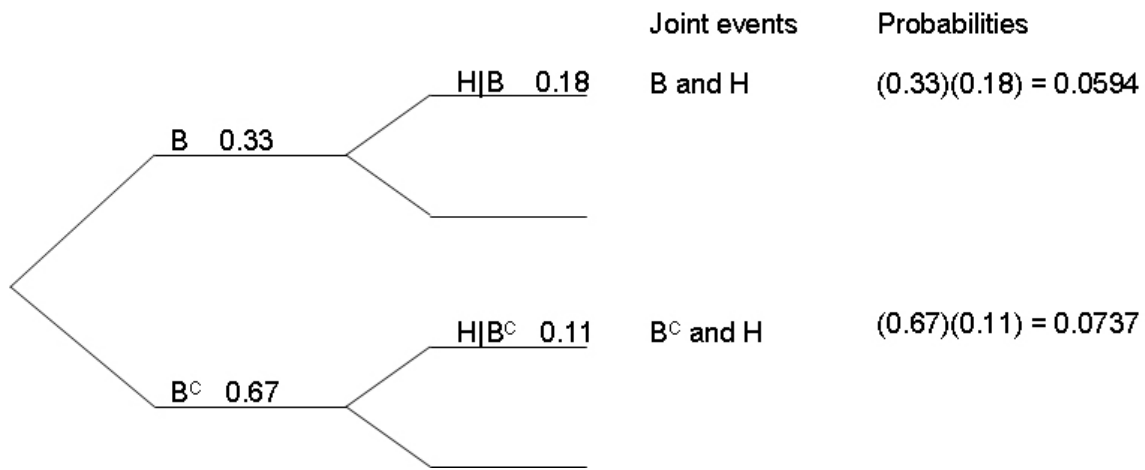
6.59



a $P(\text{vote in last election and male}) = .1806$

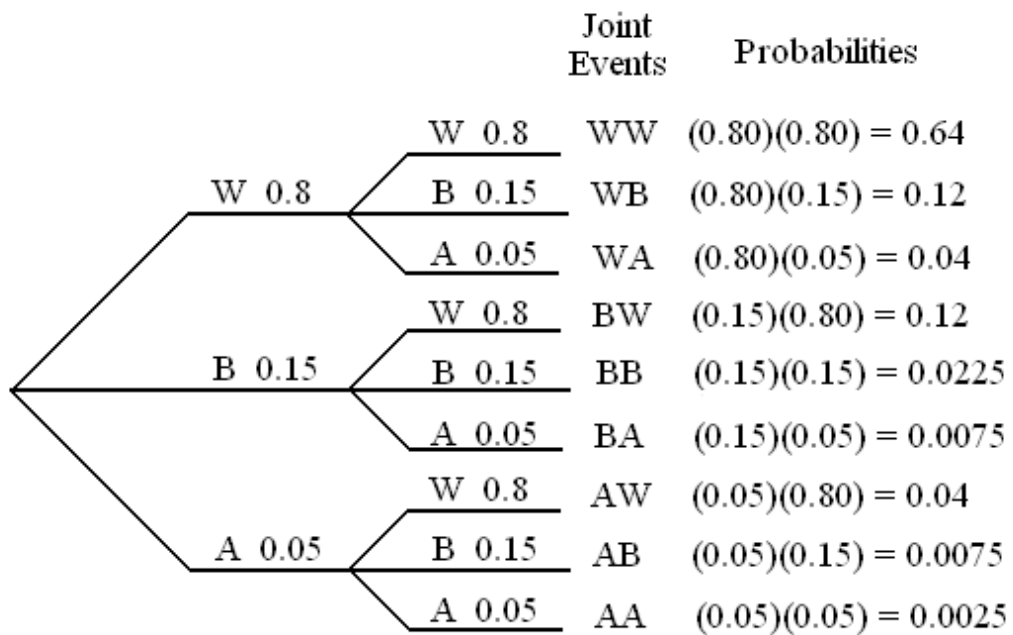
b $P(\text{vote in last election and female}) = .2494$

6.60



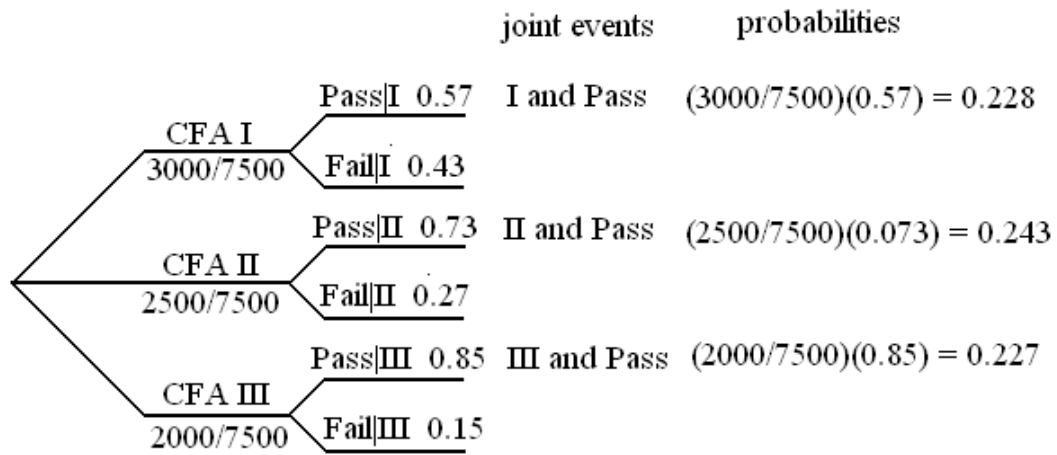
$P(\text{heart attack}) = .0594 + .0737 = .1331$

6.61



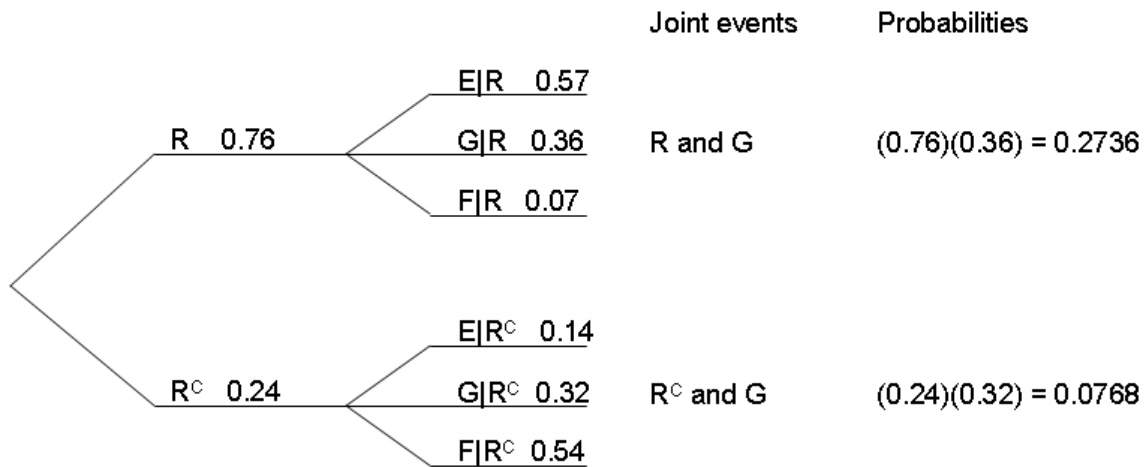
Diversity index = $.12 + .04 + .12 + .0075 + .04 + .0075 = .335$

6.62



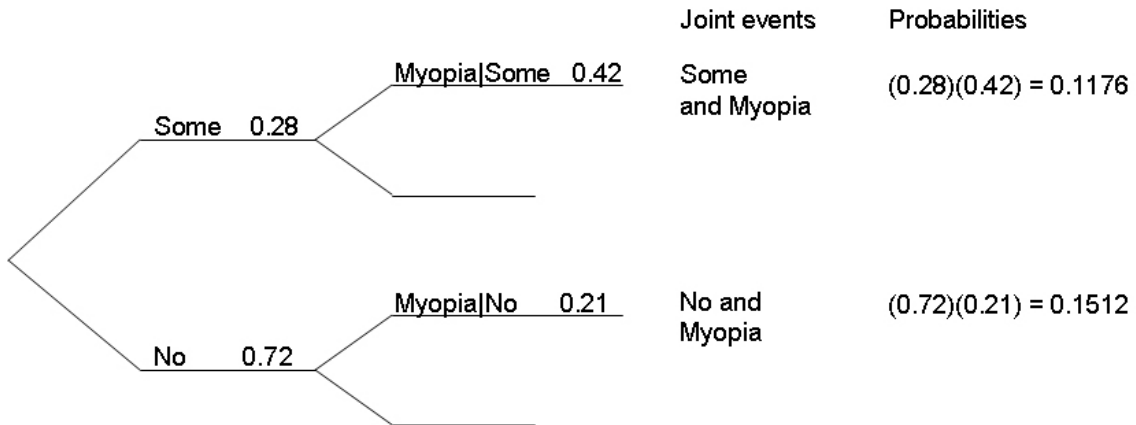
$$P(\text{pass}) = .228 + .243 + .227 = .698$$

6.63



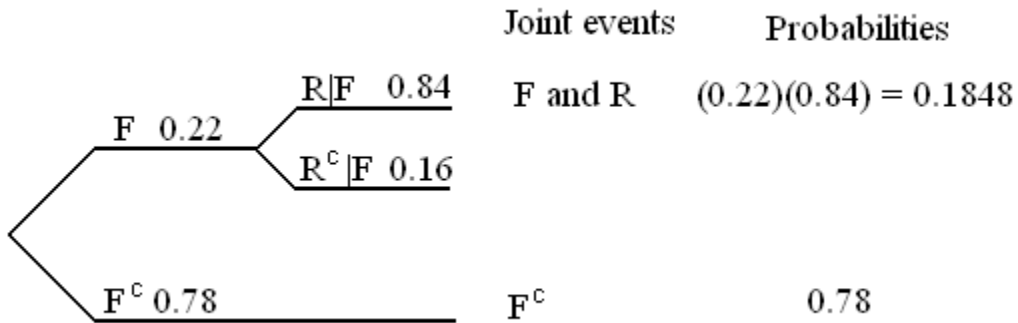
$$P(\text{good}) = .2736 + .0764 = .3504$$

6.64



$P(\text{myopic}) = .1176 + .1512 = .2688$

6.65



$P(\text{does not have to be discarded}) = .1848 + .78 = .9648$

6.66 Let A = mutual fund outperforms the market in the first year

B = mutual outperforms the market in the second year

$P(A \text{ and } B) = P(A)P(B | A) = (.15)(.22) = .033$

6.67 $P(\text{ wireless Web user uses it primarily for e-mail}) = .69$

$P(3 \text{ wireless Web users use it primarily for e-mail}) = (.69)(.69)(.69) = .3285$

6.68 Define the events:

M: The main control will fail.

B₁: The first backup will fail.

B₂: The second backup will fail

The probability that the plane will crash is

$$\begin{aligned} P(M \text{ and } B_1 \text{ and } B_2) &= [P(M)][P(B_1)][P(B_2)] \\ &= (.0001)(.01)(.01) \\ &= .00000001 \end{aligned}$$

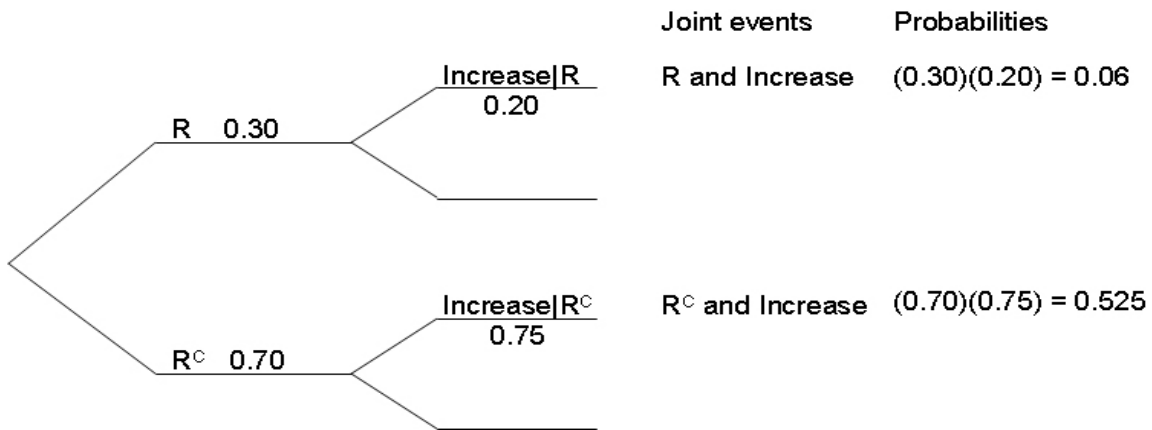
We have assumed that the 3 systems will fail independently of one another.

6.69 Let A = DJIA increase and B = NASDAQ increase

$$P(A) = .60 \text{ and } P(B | A) = .77$$

$$P(A \text{ and } B) = P(A)P(B | A) = (.60)(.77) = .462$$

6.70



$$P(\text{Increase}) = .06 + .525 = .585$$

6.71 $P(A \text{ and } B) = .36$, $P(B) = .36 + .07 = .43$

$$P(A | B) = \frac{P(A \text{ and } B)}{P(B)} = \frac{.36}{.43} = .837$$

6.72 $P(A \text{ and } B) = .32$, $P(A^C \text{ and } B) = .14$, $P(B) = .46$, $P(B^C) = .54$

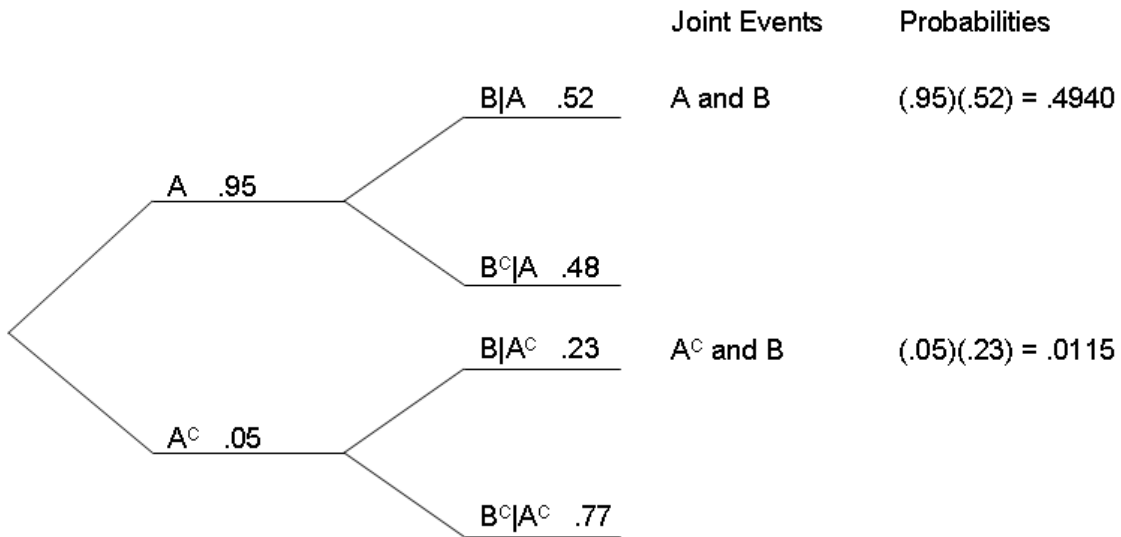
$$\text{a } P(A | B) = \frac{P(A \text{ and } B)}{P(B)} = \frac{.32}{.46} = .696$$

$$\text{b } P(A^C | B) = \frac{P(A^C \text{ and } B)}{P(B)} = \frac{.14}{.46} = .304$$

$$\text{c } P(A \text{ and } B^C) = .48; P(A | B^C) = \frac{P(A \text{ and } B^C)}{P(B^C)} = \frac{.48}{.54} = .889$$

$$\text{d } P(A^C \text{ and } B^C) = .06; P(A^C | B^C) = \frac{P(A^C \text{ and } B^C)}{P(B^C)} = \frac{.06}{.54} = .111$$

6.73



$$P(B) = .4940 + .0115 = .5055$$

$$P(A | B) = \frac{P(A \text{ and } B)}{P(B)} = \frac{.4940}{.5055} = .9773$$

$$6.74 P(F | D) = \frac{P(F \text{ and } D)}{P(D)} = \frac{.020}{.038} = .526$$

6.75 Define events: A = crash with fatality, B = BAC is greater than .09)

$$P(A) = .01, P(B | A) = .084, P(B) = .12$$

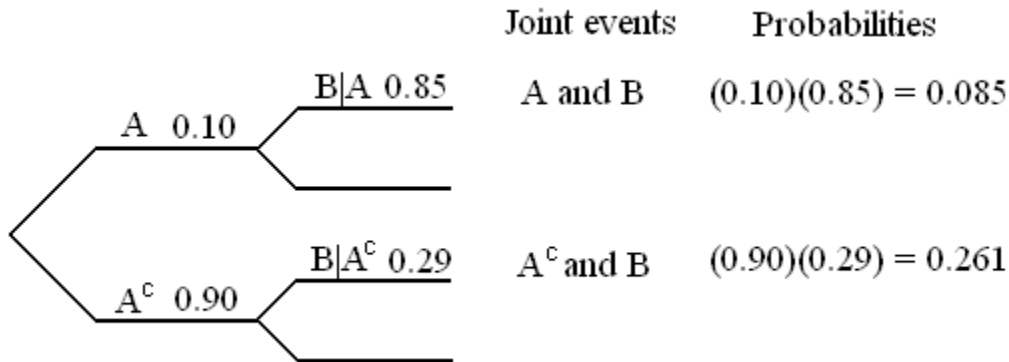
$$P(A \text{ and } B) = (.01)(.084) = .00084$$

$$P(A | B) = \frac{P(A \text{ and } B)}{P(B)} = \frac{.00084}{.12} = .007$$

$$6.76 P(\text{CFA I} | \text{passed}) = \frac{P(\text{CFA I and passed})}{P(\text{passed})} = \frac{.228}{.698} = .327$$

6.77 Define events: A = heart attack, B = periodontal disease

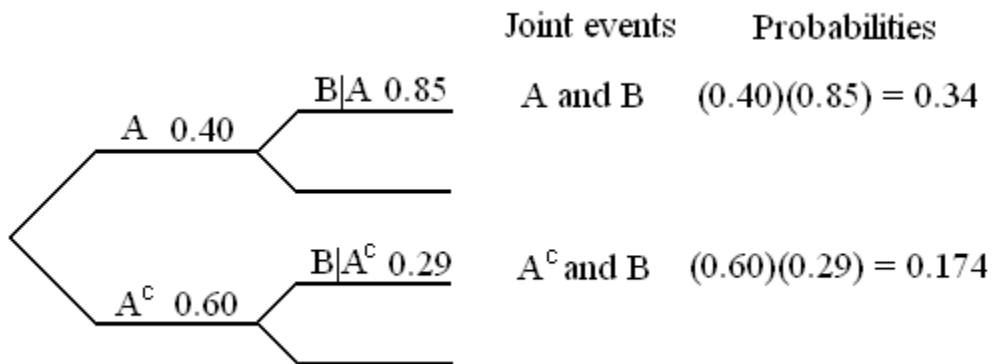
$$P(A) = .10, P(B | A) = .85, P(B | A^c) = .29$$



$$P(B) = .085 + .261 = .346$$

$$P(A | B) = \frac{P(A \text{ and } B)}{P(B)} = \frac{.085}{.346} = .246$$

6.78 $P(A) = .40$, $P(B | A) = .85$, $P(B | A^c) = .29$



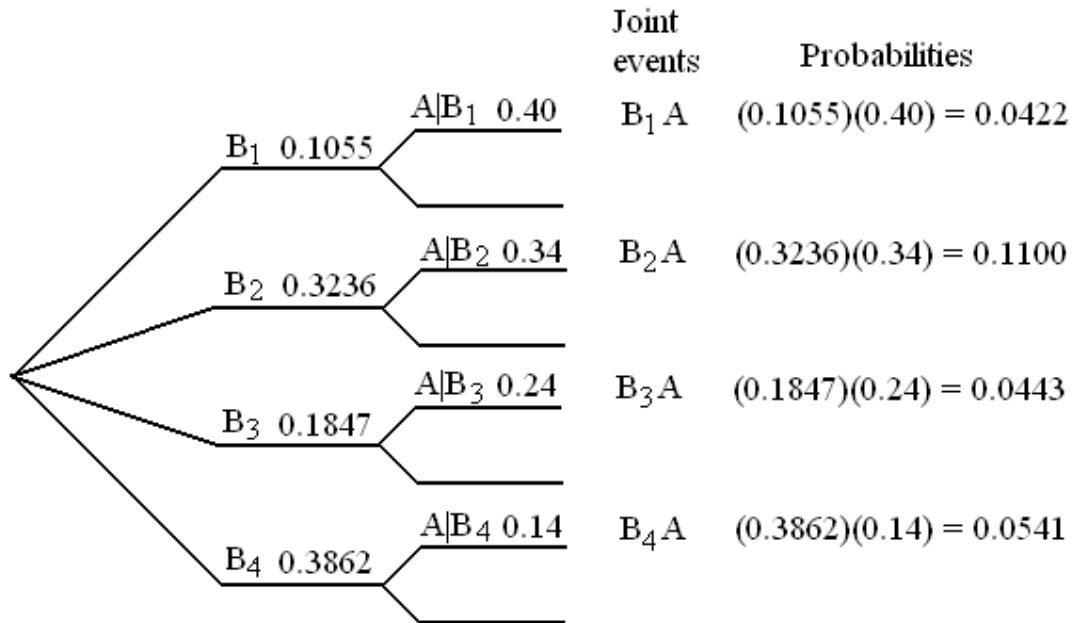
$$P(B) = .34 + .174 = .514$$

$$P(A | B) = \frac{P(A \text{ and } B)}{P(B)} = \frac{.34}{.514} = .661$$

6.79 Define events: A = smoke, B_1 = did not finish high school, B_2 = high school graduate, B_3 = some college, no degree, B_4 = completed a degree

$$P(A | B_1) = .40, P(A | B_2) = .34, P(A | B_3) = .24, P(A | B_4) = .14$$

$$\text{From Exercise 6.45: } P(B_1) = .1055, P(B_2) = .3236, P(B_3) = .1847, P(B_4) = .3862$$

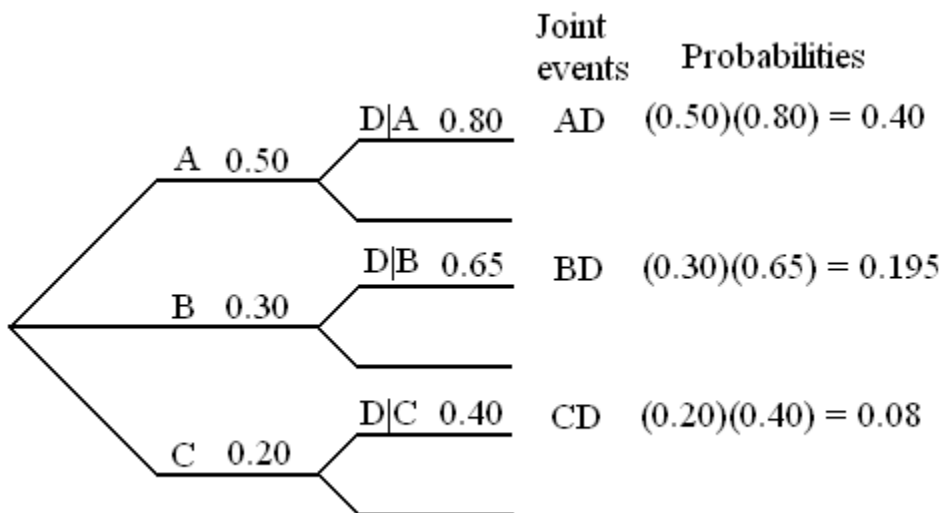


$$P(A) = .0422 + .1100 + .0443 + .0541 = .2506$$

$$P(B_4 | A) = .0541 / .2506 = .2159$$

6.80 Define events: A, B, C = airlines A, B, and C, D = on time

$$P(A) = .50, P(B) = .30, P(C) = .20, P(D | A) = .80, P(D | B) = .65, P(D | C) = .40$$

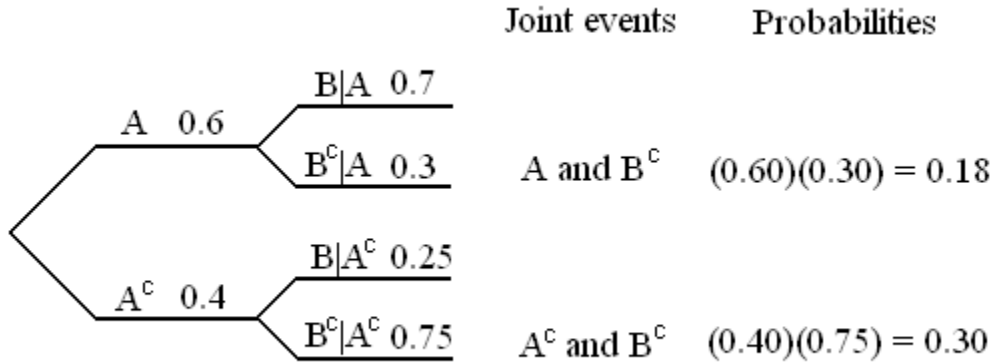


$$P(D) = .40 + .195 + .08 = .675$$

$$P(A | D) = \frac{P(A \text{ and } D)}{P(D)} = \frac{.40}{.675} = .593$$

6.81 Define events: A = win series, B = win first game

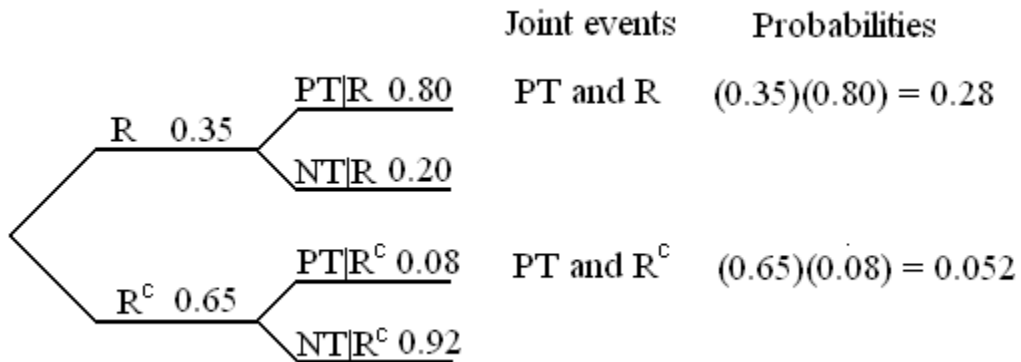
$$P(A) = .60, P(B | A) = .70, P(B | A^c) = .25$$



$$P(B^c) = .18 + .30 = .48$$

$$P(A | B^c) = \frac{P(A \text{ and } B^c)}{P(B^c)} = \frac{.18}{.48} = .375$$

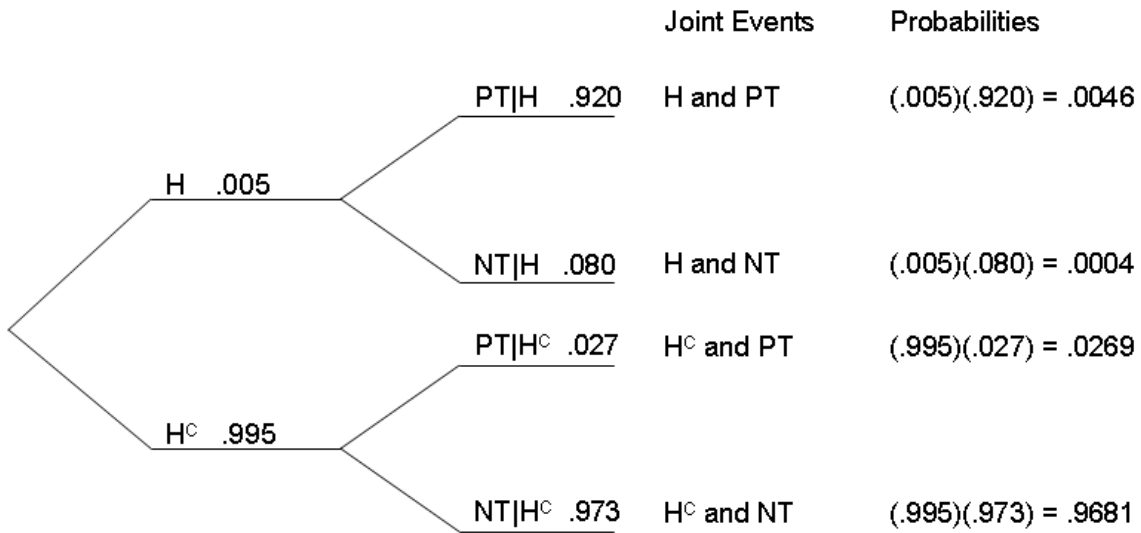
6.82



$$P(PT) = .28 + .052 = .332$$

$$P(R | PT) = \frac{P(R \text{ and } PT)}{P(PT)} = \frac{.28}{.332} = .843$$

6.83



$$P(\text{PT}) = .0046 + .0269 = .0315$$

$$P(\text{H} | \text{PT}) = \frac{P(\text{H and PT})}{P(\text{PT})} = \frac{.0046}{.0315} = .1460$$

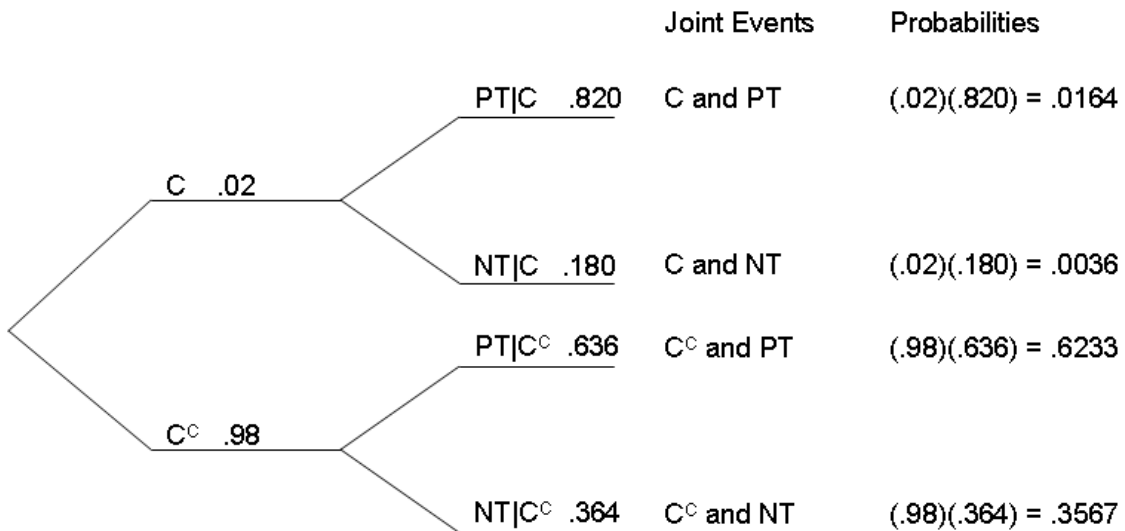
$$6.84 \text{ Sensitivity} = P(\text{PT} | \text{H}) = .920$$

$$\text{Specificity} = P(\text{NT} | \text{H}^{\text{C}}) = .973$$

$$\text{Positive predictive value} = P(\text{H} | \text{PT}) = .1460$$

$$\text{Negative predictive value} = P(\text{H}^{\text{C}} | \text{NT}) = \frac{P(\text{H}^{\text{C}} \text{ and NT})}{P(\text{NT})} = \frac{.9681}{.0004 + .9681} = \frac{.9681}{.9685} = .9996$$

6.85



$$P(\text{PT}) = .0164 + .6233 = .6397$$

$$P(NT) = .0036 + .3567 = .3603$$

$$P(C | PT) = \frac{P(C \text{ and } PT)}{P(PT)} = \frac{.0164}{.6397} = .0256$$

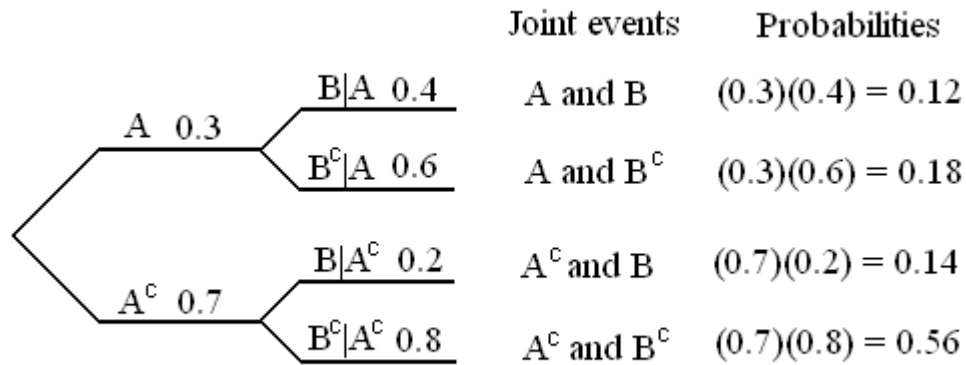
$$P(C | NT) = \frac{P(C \text{ and } NT)}{P(NT)} = \frac{.0036}{.3603} = .0010$$

6.86 a $P(\text{Marketing-A}) = .06 + .23 = .29$

b $P(\text{Marketing A} | \text{Statistics not A}) = \frac{P(\text{Marketing A and Statistics not A})}{P(\text{Statistics not A})} = \frac{.23}{.23 + .58} = \frac{.23}{.81} = .2840$

c No, the probabilities in (a) and (b) differ

6.87 Define events: A = win contract A and B = win contract B



a $P(A \text{ and } B) = .12$

b $P(A \text{ and } B^c) + P(A^c \text{ and } B) = .18 + .14 = .32$

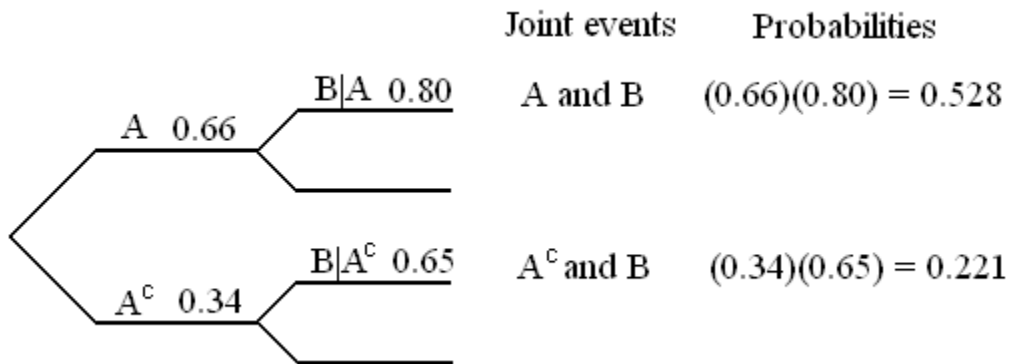
c $P(A \text{ and } B) + P(A \text{ and } B^c) + P(A^c \text{ and } B) = .12 + .18 + .14 = .44$

6.88 a $P(\text{second}) = .05 + .14 = .19$

b $P(\text{successful} | -8 \text{ or less}) = \frac{P(\text{successful and } -8 \text{ or less})}{P(-8 \text{ or less})} = \frac{.15}{.15 + .14} = \frac{.15}{.29} = .517$

c No, because $P(\text{successful}) = .66 + .15 = .81$, which is not equal to $P(\text{successful} | -8 \text{ or less})$.

6.89 Define events: A = woman, B = drug is effective



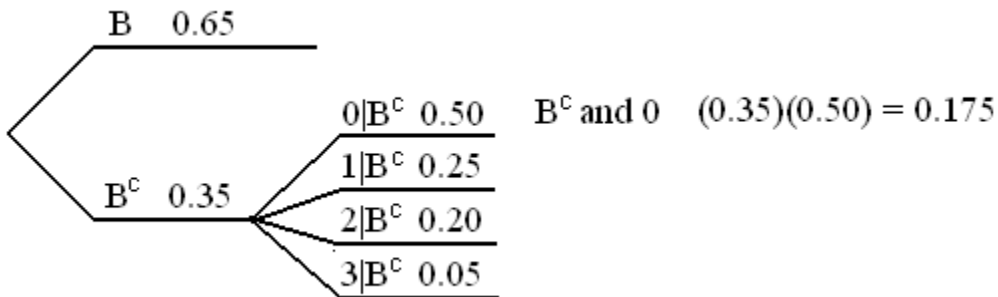
$$P(B) = .528 + .221 = .749$$

$$6.90 P(A^c | B) = \frac{P(A^c \text{ and } B)}{P(B)} = \frac{.221}{.749} = .295$$

6.91 P(Idle roughly)

$$= P(\text{at least one spark plug malfunctions}) = 1 - P(\text{all function}) = 1 - (.90^4) = 1 - .6561 = .3439$$

6.92



$$P(\text{no sale}) = .65 + .175 = .825$$

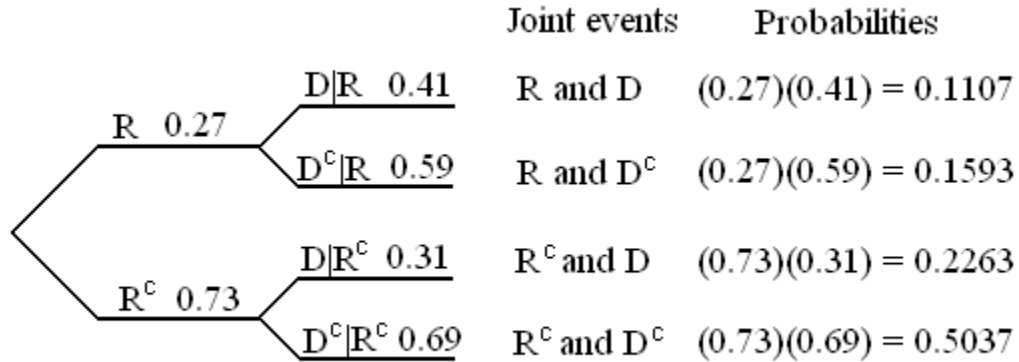
$$6.93 \text{ a } P(\text{pass}) = .86 + .03 = .89$$

$$\text{b } P(\text{pass} | \text{miss 5 or more classes}) = \frac{P(\text{pass and miss 5 or more classes})}{P(\text{miss 5 or more classes})} = \frac{.03}{.09 + .03} = \frac{.03}{.12} = .250$$

$$\text{c } P(\text{pass} | \text{miss less than 5 classes}) = \frac{P(\text{pass and miss less than 5 classes})}{P(\text{miss less than 5 classes})} = \frac{.86}{.86 + .02} = \frac{.86}{.88} = .977$$

d No since $P(\text{pass}) \neq P(\text{pass} | \text{miss 5 or more classes})$

6.94



a $P(D) = P(R \text{ and } D) + P(R^c \text{ and } D) = .1107 + .2263 = .3370$

$$P(R|D) = \frac{P(R \text{ and } D)}{P(D)} = \frac{.1107}{.3370} = .3285$$

b $P(D^c) = P(R \text{ and } D^c) + P(R^c \text{ and } D^c) = .1593 + .5037 = .6630$

$$P(R|D^c) = \frac{P(R \text{ and } D^c)}{P(D^c)} = \frac{.1593}{.6630} = .2403$$

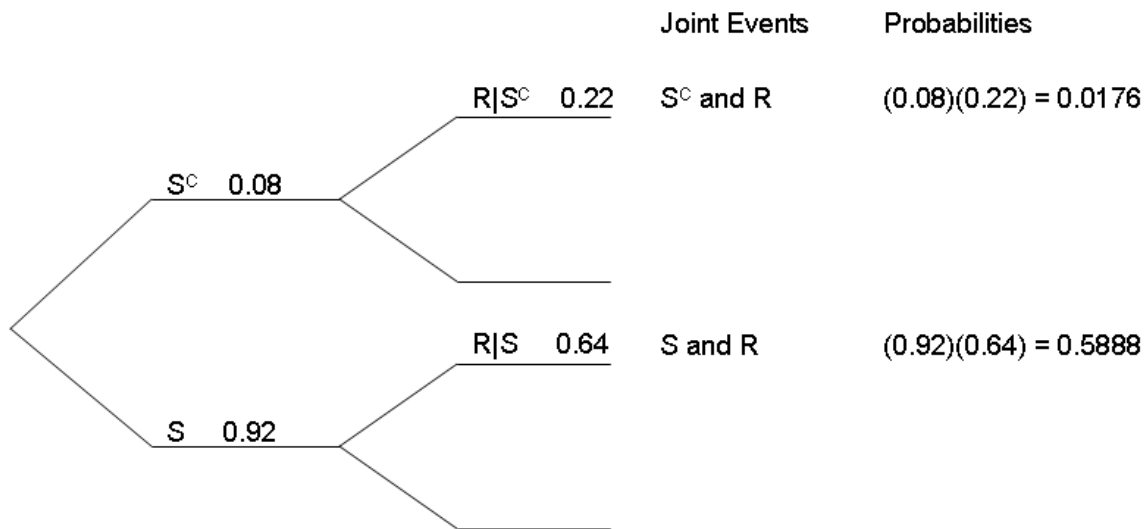
6.95 a $P(\text{excellent}) = .27 + .22 = .49$

b $P(\text{excellent} | \text{man}) = .22 / (.22 + .10 + .12 + .06) = .44$

$$c P(\text{man} | \text{excellent}) = \frac{P(\text{man and excellent})}{P(\text{excellent})} = \frac{.22}{.27 + .22} = \frac{.22}{.49} = .449$$

d No, since $P(\text{excellent}) \neq P(\text{excellent} | \text{man})$

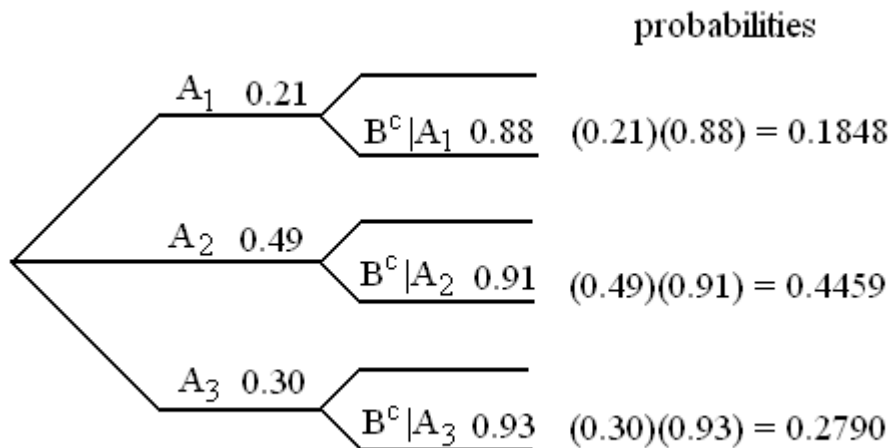
6.96



$$P(R) = .0176 + .5888 = .6064$$

$$P(S | R) = \frac{P(S \text{ and } R)}{P(R)} = \frac{.5888}{.6064} = .9710$$

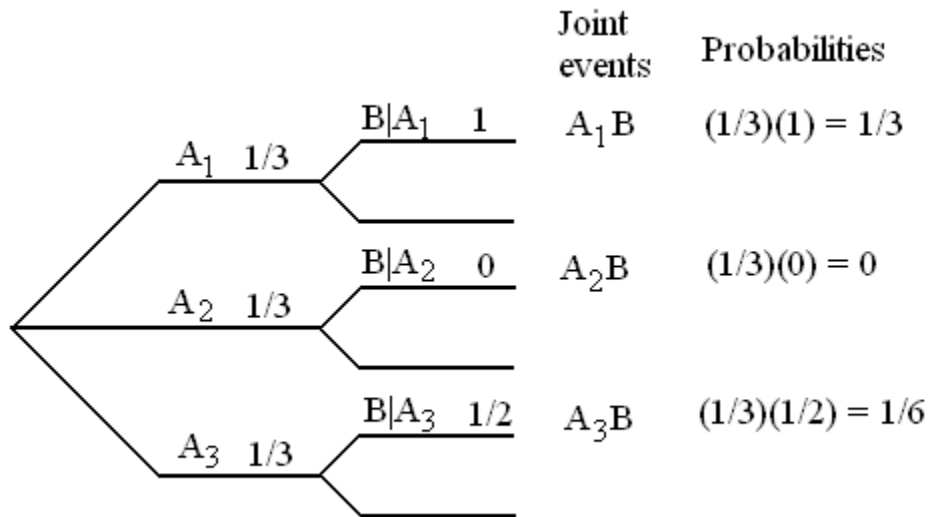
6.97 Define events: A_1 = Low-income earner, A_2 = medium-income earner, A_3 = high-income earner, B = die of a heart attack



$$P(B^c) = .1848 + .4459 + .2790 = .9097$$

$$P(A_1 | B^c) = \frac{P(A_1 \text{ and } B^c)}{P(B^c)} = \frac{.1848}{.9097} = .2031$$

6.98 Define the events: A_1 = envelope containing two Maui brochures is selected, A_2 = envelope containing two Oahu brochures is selected, A_3 = envelope containing one Maui and one Oahu brochures is selected. B = a Maui brochure is removed from the selected envelope.



$$P(B) = 1/3 + 0 + 1/6 = 1/2$$

$$P(A_1 | B) = \frac{P(A_1 \text{ and } B)}{P(B)} = \frac{1/3}{1/2} = 2/3$$

6.99 Define events: A = purchase extended warranty, B = regular price

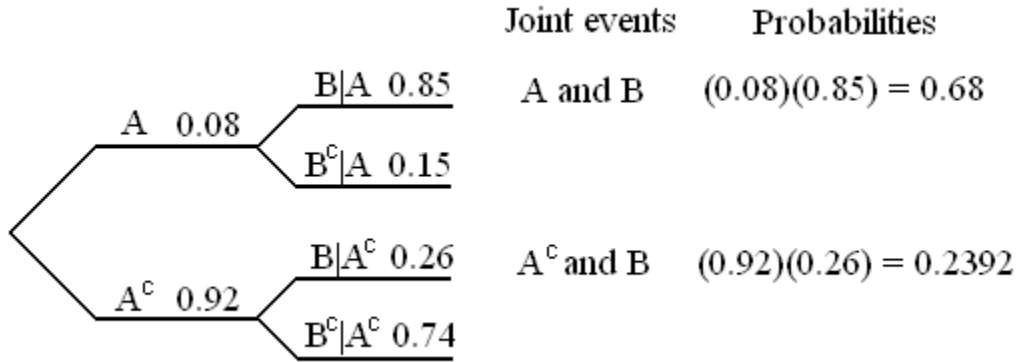
$$a \ P(A | B) = \frac{P(A \text{ and } B)}{P(B)} = \frac{.21}{.21 + .57} = \frac{.21}{.78} = .2692$$

$$b \ P(A) = .21 + .14 = .35$$

c No, because $P(A) \neq P(A | B)$

6.100 Define events: A = company fail, B = predict bankruptcy

$$P(A) = .08, P(B | A) = .85, P(B^c | A^c) = .74$$



$$P(B) = .068 + .2392 = .3072$$

$$P(A | B) = \frac{P(A \text{ and } B)}{P(B)} = \frac{.068}{.3072} = .2214$$

6.101 Define events: A = job security is an important issue, B = pension benefits is an important issue

$$P(A) = .74, P(B) = .65, P(A | B) = .60$$

$$a) P(A \text{ and } B) = P(B)P(A | B) = (.65)(.60) = .39$$

$$b) P(A \text{ or } B) = .74 + .65 - .39 = 1$$

6.102 Probabilities of outcomes: $P(HH) = .25, P(HT) = .25, P(TH) = .25, P(TT) = .25$

$$P(TT | HH \text{ is not possible}) = .25 / (.25 + .25 + .25) = .333$$

$$6.103 P(T) = .5$$

Case 6.1

$$1. P(\text{Curtain A}) = 1/3, P(\text{Curtain B}) = 1/3$$

$$2. P(\text{Curtain A}) = 1/3, P(\text{Curtain B}) = 2/3$$

Case 6.2

Outcome	Probability of outcome	Bases Occupied	Outs	Probability of scoring	Joint Probability
1	.75	2nd	1	.42	.3150
2	.10	1st	1	.26	.0260
3	.10	none	2	.07	.0070
4	.05	1st and 2nd	0	.59	.0295

$$P(\text{scoring}) = .3775$$

Because the probability of scoring with a runner on first base with no outs (.39) is greater than the probability of scoring after bunting (.3775) you should not bunt.

Case 6.3

0 outs:

Probability of scoring any runs from first base = .39

Probability of scoring from second base = probability of successful steal \times probability of scoring any runs from second base = $(.68)(.57) = .3876$

Decision: Do not attempt to steal.

1 out:

Probability of scoring any runs from first base = .26

Probability of scoring from second base = probability of successful steal \times probability of scoring any runs from second base = $(.68) \times (.42) = .2856$

Decision: Attempt to steal.

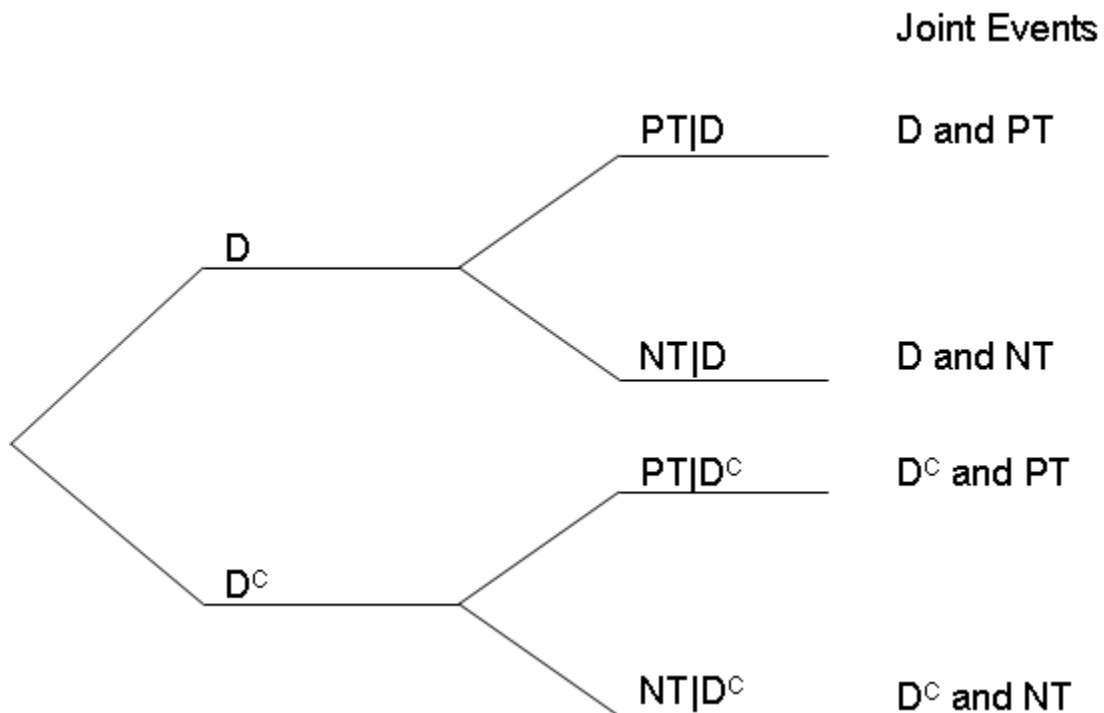
2 outs:

Probability of scoring any runs from first base = .13

Probability of scoring from second base = probability of successful steal \times probability of scoring any runs from second base = $(.68) \times (.24) = .1632$

Decision: Attempt to steal.

Case 6.4



Age 25: $P(D) = 1/1,300$

$P(D \text{ and } PT) = (1/1,300)(.624) = .00048$

$P(D \text{ and } NT) = (1/1,300)(.376) = .00029$

$P(D^C \text{ and } PT) = (1,299/1,300)(.04) = .03997$

$P(D^C \text{ and } NT) = (1,299/1,300)(.96) = .95926$

$P(PT) = .00048 + .03997 = .04045$

$P(NT) = .00029 + .95926 = .95955$

$P(D | PT) = .00048/.04045 = .01187$

$P(D | NT) = .00029/.95955 = .00030$

Age 30: $P(D) = 1/900$

$P(D \text{ and } PT) = (1/900)(.710) = .00079$

$P(D \text{ and } NT) = (1/900)(.290) = .00032$

$P(D^C \text{ and } PT) = (899/900)(.082) = .08190$

$P(D^C \text{ and } NT) = (899/900)(.918) = .91698$

$P(PT) = .00079 + .08190 = .08269$

$P(NT) = .00032 + .91698 = .91730$

$P(D | PT) = .00079/.08269 = .00955$

$P(D | NT) = .00032/.91730 = .00035$

Age 35: $P(D) = 1/350$

$P(D \text{ and } PT) = (1/350)(.731) = .00209$

$P(D \text{ and } NT) = (1/350)(.269) = .00077$

$P(D^C \text{ and } PT) = (349/350)(.178) = .17749$

$P(D^C \text{ and } NT) = (349/350)(.822) = .81965$

$P(PT) = .00209 + .17749 = .17958$

$P(NT) = .00077 + .81965 = .82042$

$P(D | PT) = .00209/.17958 = .01163$

$P(D | NT) = .00077/.82042 = .00094$

Age 40: $P(D) = 1/100$

$P(D \text{ and } PT) = (1/100)(.971) = .00971$

$P(D \text{ and } NT) = (1/100)(.029) = .00029$

$P(D^C \text{ and } PT) = (99/100)(.343) = .33957$

$P(D^C \text{ and } NT) = (99/100)(.657) = .65043$

$P(PT) = .00971 + .33957 = .34928$

$$P(\text{NT}) = .00029 + .65043 = .65072$$

$$P(\text{D} \mid \text{PT}) = .00971 / .34928 = .02780$$

$$P(\text{D} \mid \text{NT}) = .00029 / .65072 = .00045$$

$$\text{Age 45: } P(\text{D}) = 1/25$$

$$P(\text{D and PT}) = (1/25)(.971) = .03884$$

$$P(\text{D and NT}) = (1/25)(.029) = .00116$$

$$P(\text{D}^{\text{C}} \text{ and PT}) = (24/25)(.343) = .32928$$

$$P(\text{D}^{\text{C}} \text{ and NT}) = (24/25)(.657) = .63072$$

$$P(\text{PT}) = .03884 + .32928 = .36812$$

$$P(\text{NT}) = .00116 + .63072 = .63188$$

$$P(\text{D} \mid \text{PT}) = .03884 / .36812 = .10551$$

$$P(\text{D} \mid \text{NT}) = .00116 / .63188 = .00184$$

$$\text{Age 49: } P(\text{D}) = 1/12$$

$$P(\text{D and PT}) = (1/12)(.971) = .08092$$

$$P(\text{D and NT}) = (1/12)(.029) = .00242$$

$$P(\text{D}^{\text{C}} \text{ and PT}) = (11/12)(.343) = .31442$$

$$P(\text{D}^{\text{C}} \text{ and NT}) = (11/12)(.657) = .60255$$

$$P(\text{PT}) = .08092 + .31442 = .39533$$

$$P(\text{NT}) = .00242 + .60255 = .60467$$

$$P(\text{D} \mid \text{PT}) = .08092 / .39533 = .20468$$

$$P(\text{D} \mid \text{NT}) = .00242 / .60467 = .00400$$