

## Modulo Operation (mod) Algorithm and Examples

In computing, the modulo (sometimes called modulus, or mod) operation finds the remainder of division of one number by another. Given two positive numbers,  $a$  (the dividend) and  $n$  (the divisor), a modulo  $n$  (abbreviated as  $a \bmod n$ ) is the remainder of the Euclidean division of  $a$  by  $n$ . For instance, the expression "5 mod 2" would evaluate to 1 because 5 divided by 2 leaves a quotient of 2 and a remainder of 1, while "9 mod 3" would evaluate to 0 because the division of 9 by 3 has a quotient of 3 and leaves a remainder of 0; there is nothing to subtract from 9 after multiplying 3 times 3. Note that doing the division with a calculator won't show the result referred to here by this operation; the quotient will be expressed as a decimal fraction. Although typically performed with  $a$  and  $n$  both being integers, many computing systems allow other types of numeric operands. The range of numbers for an integer modulo of  $n$  is 0 to  $n - 1$ . ( $n \bmod 1$  is always 0;  $n \bmod 0$  is undefined, possibly resulting in a "Division by zero" error in computer programming languages) See modular arithmetic for an older and related convention applied in number theory. When either  $a$  or  $n$  is negative, the naive definition breaks down and programming languages differ in how these values are defined.

Example 1.  $a \bmod n \equiv a - [n \times \text{int}(\frac{a}{n})]$

$$\begin{aligned} & [269.86] - [n \times \text{int}(\frac{a}{n})] \\ &= 269 - [100 \times \text{int}(\frac{269.86}{100})] \\ &= 269 - [100 \times \text{int}(2.6986)] \\ &= 269 - [100 \times 2] \\ &= 69 \end{aligned}$$

Example 2.  $M_t^b \equiv [100 \times 10^{(\log P_t) \bmod 1}] \bmod 100$

$$\begin{aligned} & (\log P_t) \bmod 1 \\ &= \log(269.86) \bmod 1 \\ \text{Step 1.} &= 2.4311 \bmod 1 \\ &= 2.4311 - [1 \times \text{int}(\frac{2.4311}{1})] \\ &= 2.4311 - 2 \\ &= 0.4311 \end{aligned}$$

$$\begin{aligned} & \text{Step 2.} \\ & M_t^b = [100 \times 10^{0.4311}] \bmod 100 \\ &= [100 \times 2.6983] \bmod 100 \\ &= 269.83 - [100 \times \text{int}(\frac{269.83}{100})] \\ &= 269.83 - 200 \\ &= 69 \end{aligned}$$